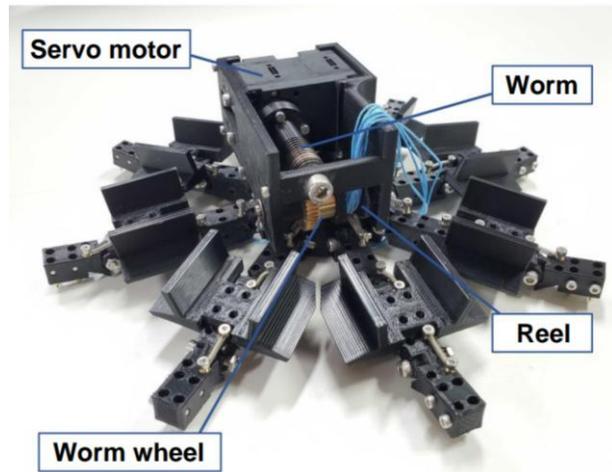


# GRIEEL: The Gripper-Wheel Transformable Module

## GRIEEL

GRipper      whEEL





**POLITECNICO**  
MILANO 1863



**TOHOKU**  
UNIVERSITY



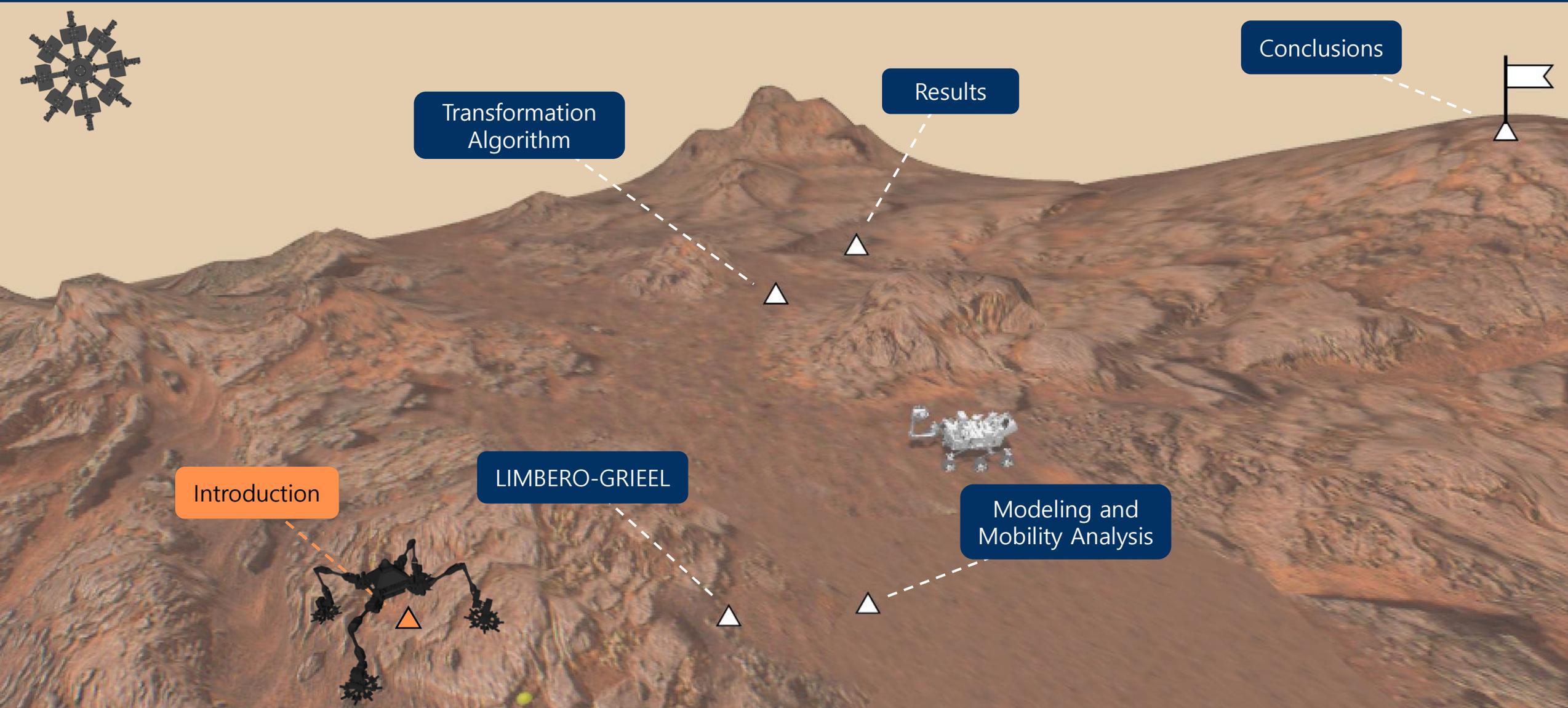
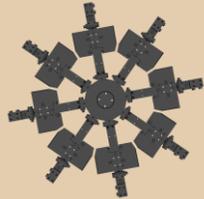
03/04/2025, Milano

# Motion Control and Manipulability Analysis of LIMBERO-GRIEEL: a Multimodal Limbed Robot for Unstructured Environments



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MSc in Automation and Control  
Engineering  
Academic year: 2024-2025

**Advisor** Prof. Luca Bascetta  
**Co-advisor** Prof. Yoshida Kazuya



Introduction

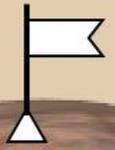
Transformation  
Algorithm

Results

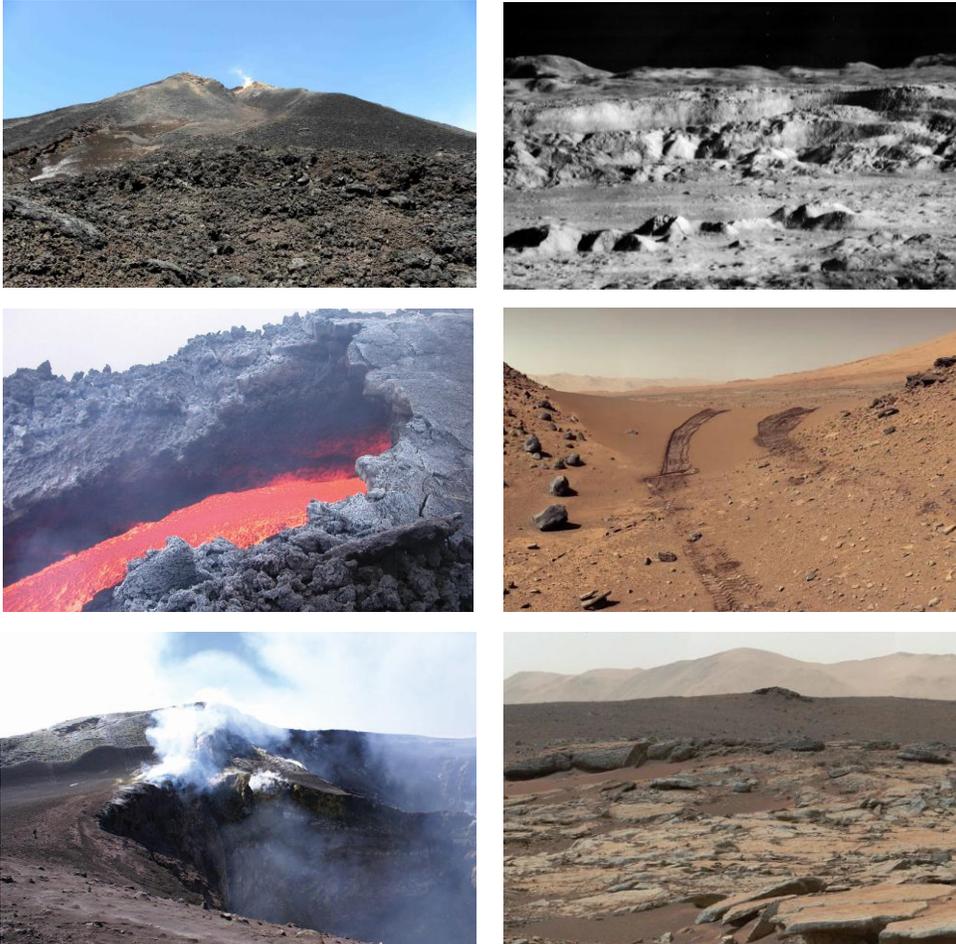
Conclusions

LIMBERO-GRIEEL

Modeling and  
Mobility Analysis



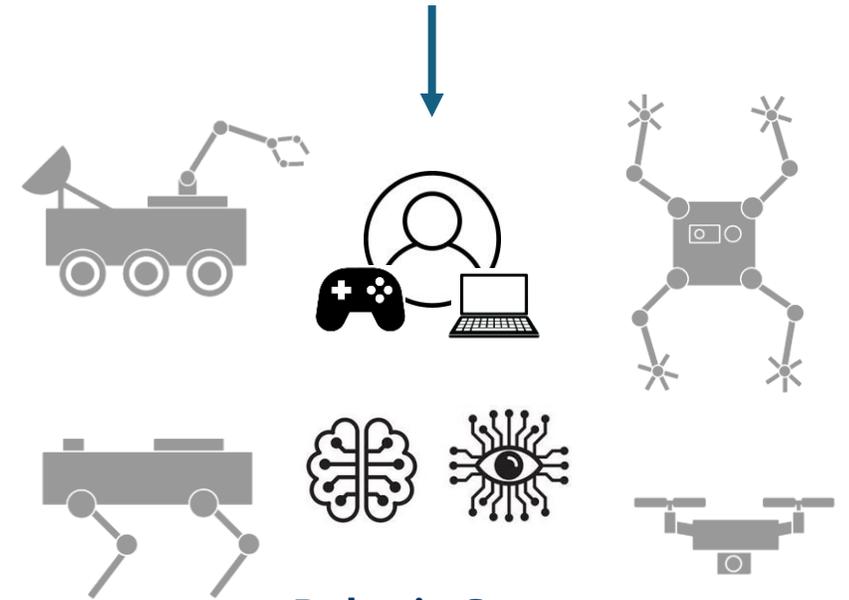
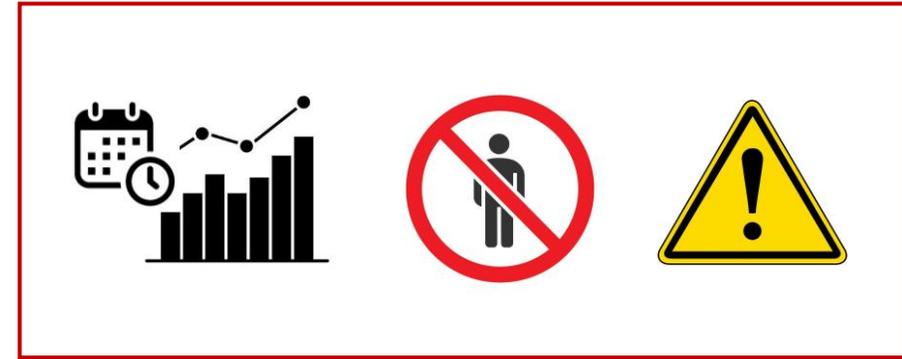
## Monitoring and Exploration



## Disaster response

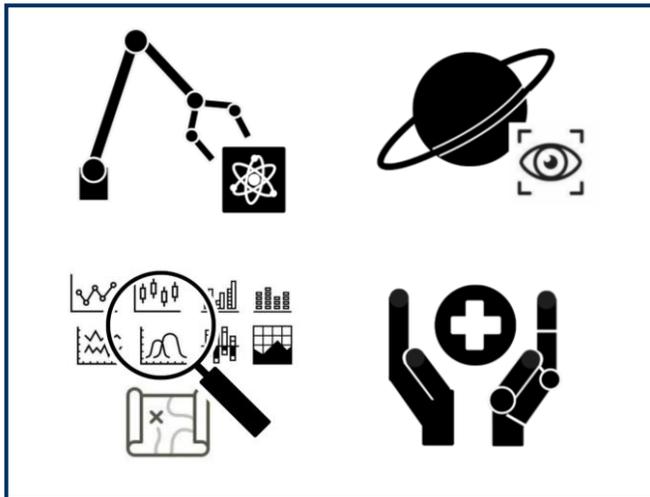


## Challenges



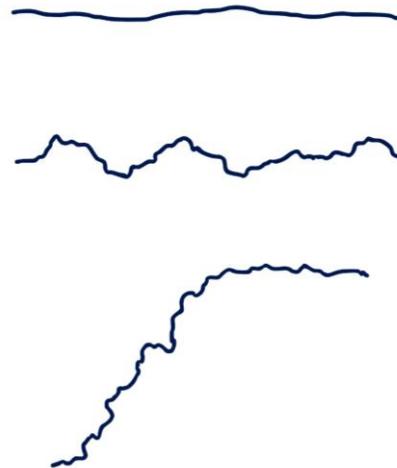
## Robotic Systems

### Robot's tasks

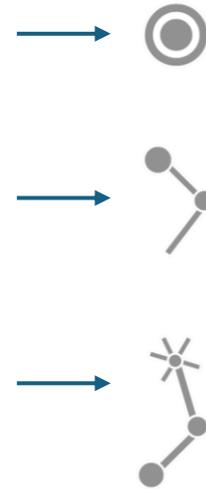


- Collection of scientific samples
- Exploration of extreme environments
- Gathering of environmental data
- Safe and Rescue missions

### Different terrains



### Optimal locomotion



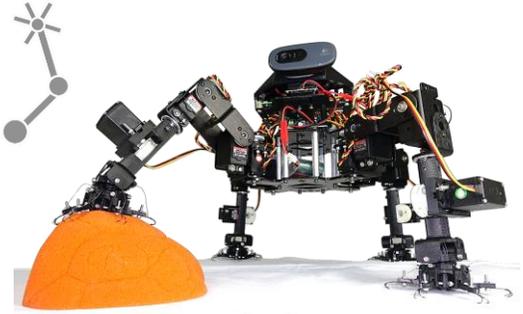
### ✗ Classical Robotic systems

- Limited traversability
- Single purpose
- Multirobot coordination

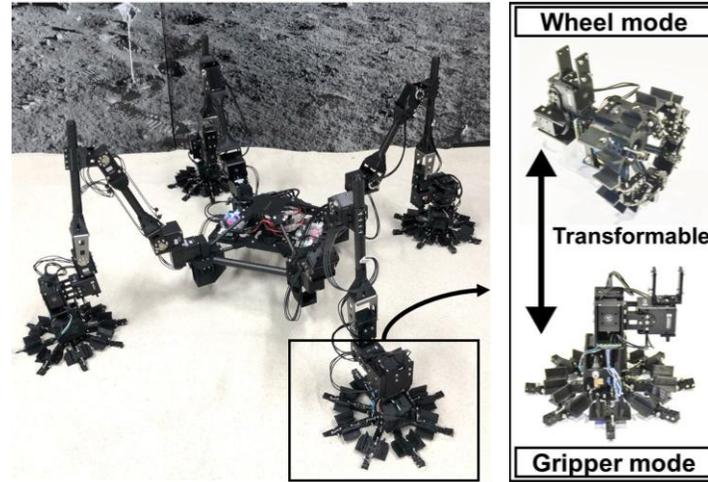
### ✓ Multimodal Robots

- Higher traversability
- Multipurpose machines

## Climbing locomotion



## LIMBERO-GRIEEL

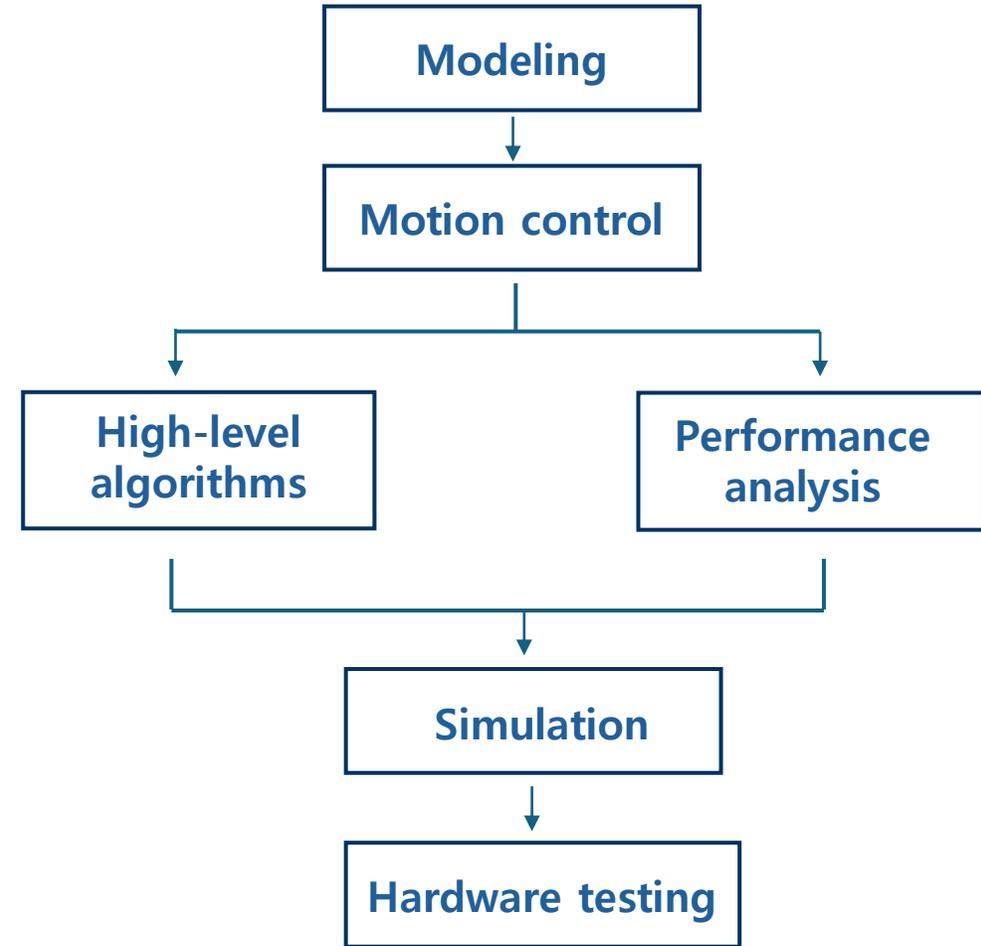


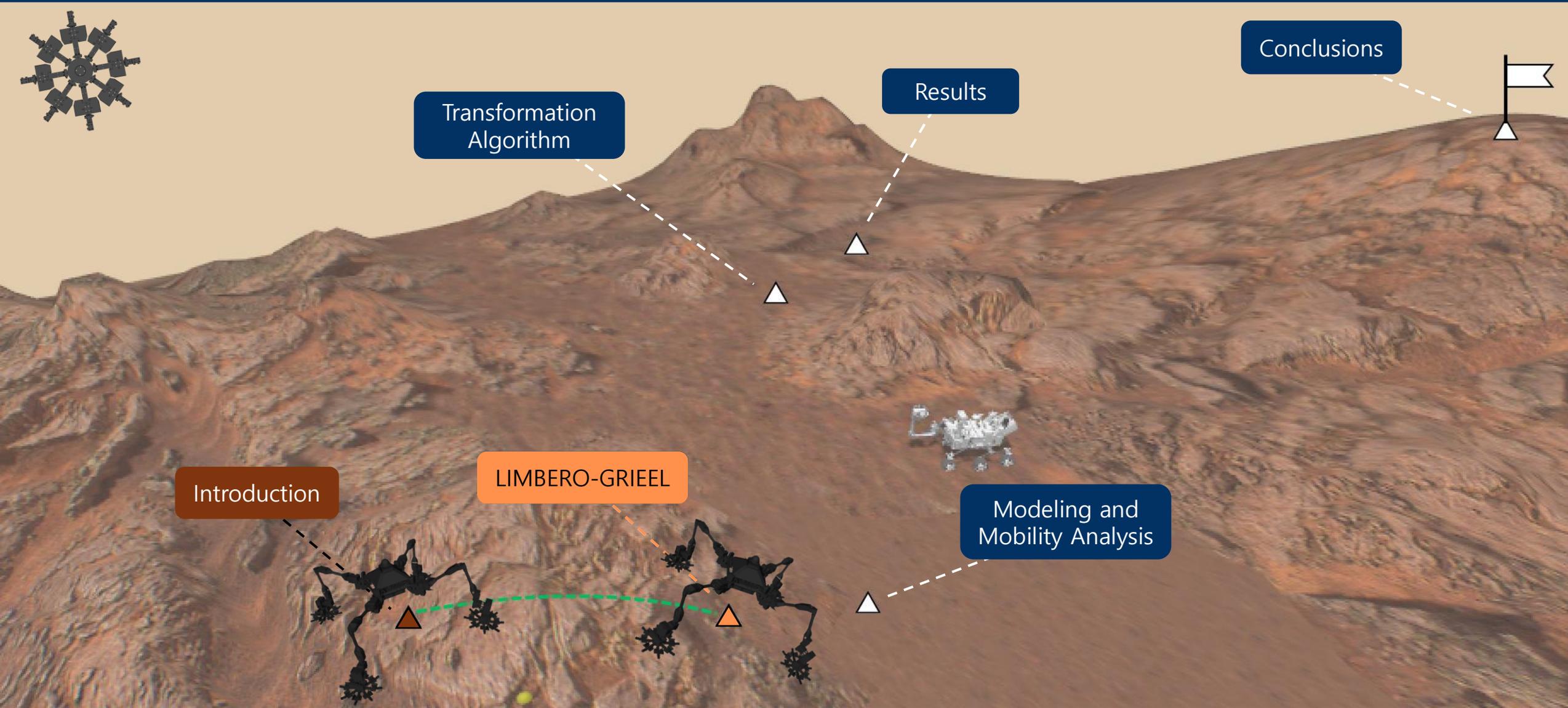
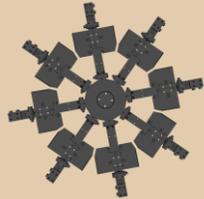
Multilimbed Multimodal gripper-wheel mobile robot

- Wheeled locomotion
- Climbing locomotion
- Walking locomotion
- Manipulation



Wheeled locomotion





Introduction

LIMBERO-GRIEEL

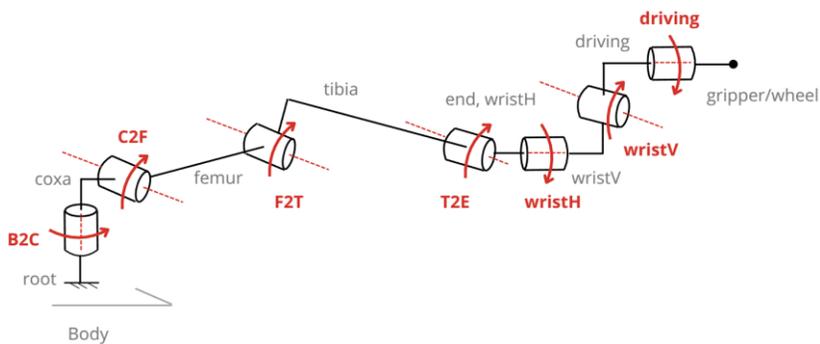
Transformation Algorithm

Results

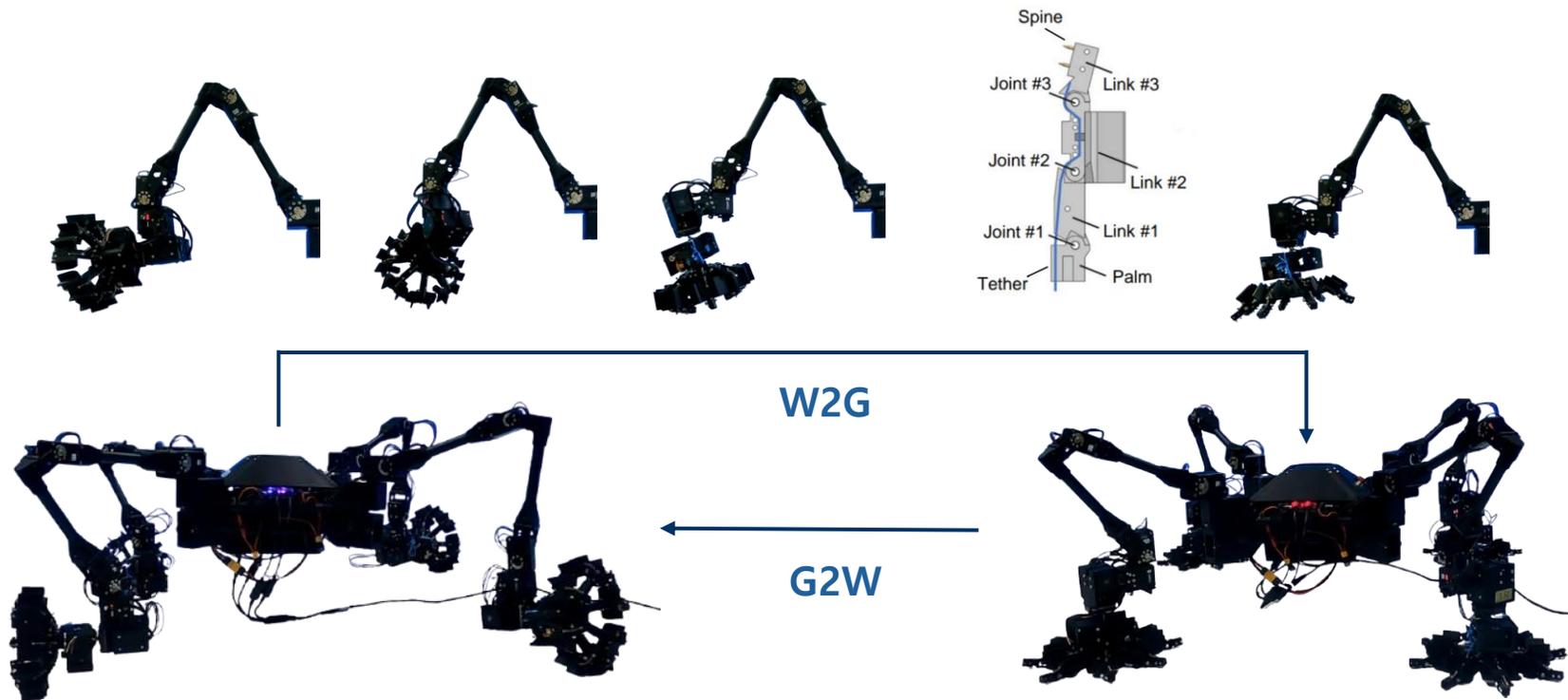
Conclusions

Modeling and Mobility Analysis

## Limb DOFs



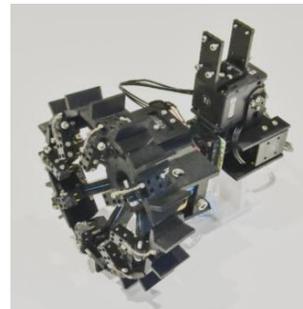
7 Degrees of freedom (DOFs)  
+ Locking motor



### Wheel Mode

$$\text{wristH} = \pi$$

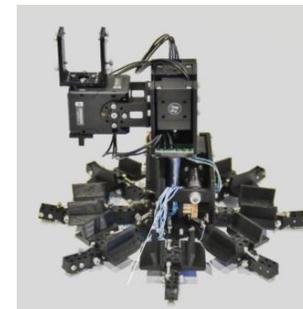
$$\text{wristV} = \pi/2$$



### Gripper Mode

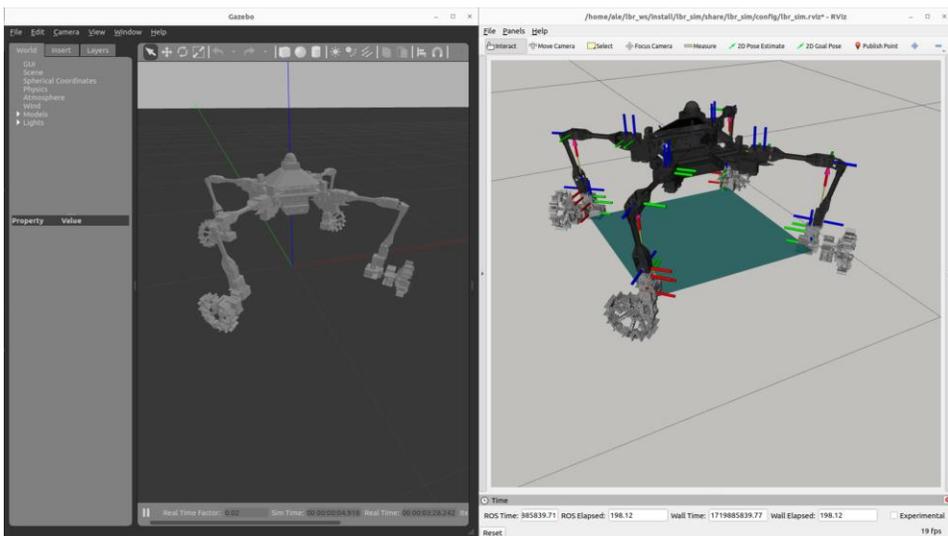
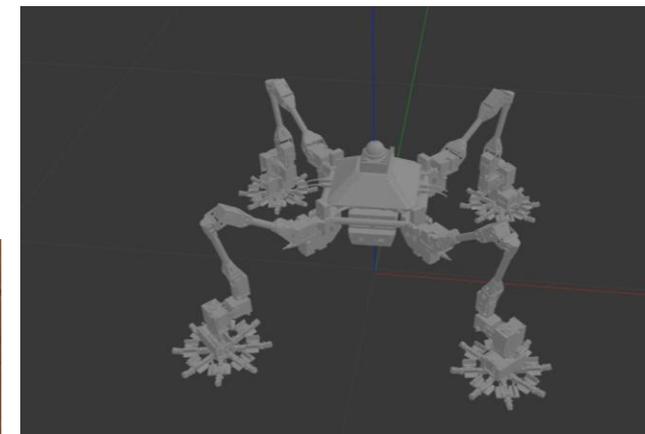
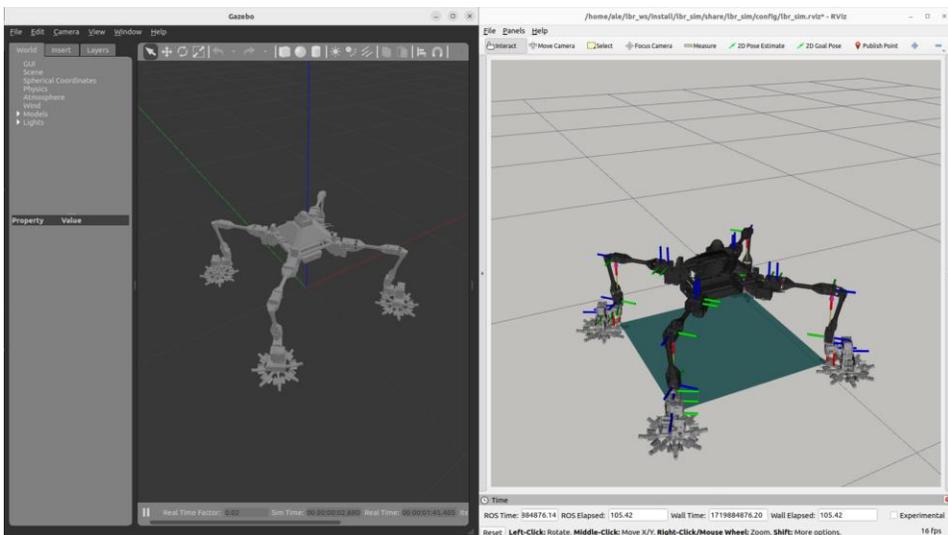
$$\text{wristH} = 0$$

$$\text{wristV} = 0$$

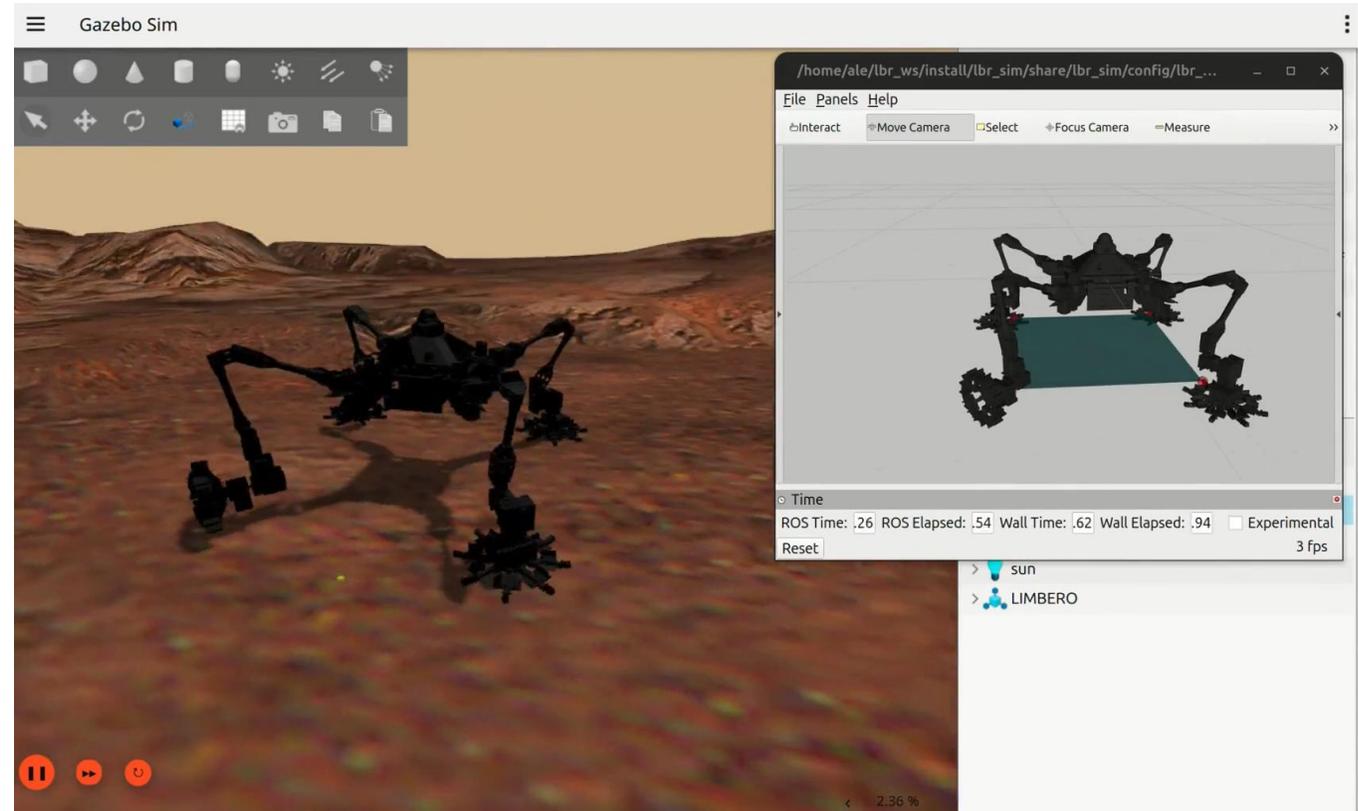
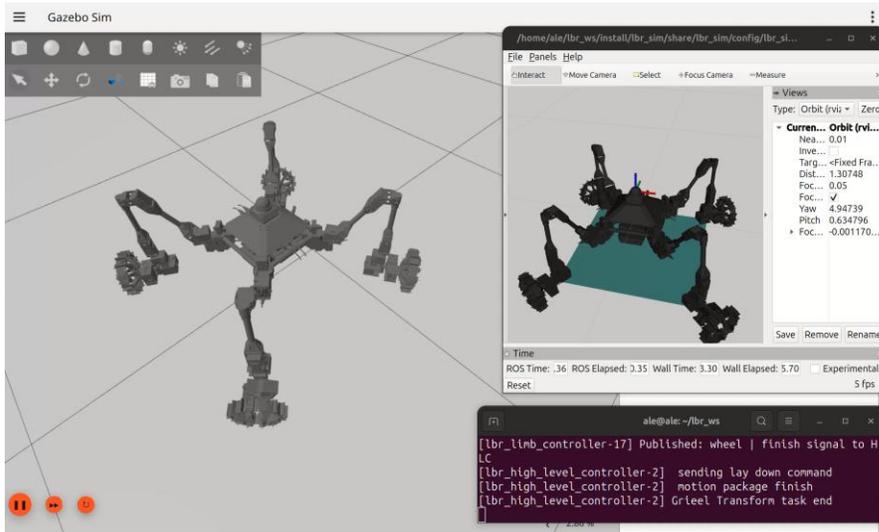
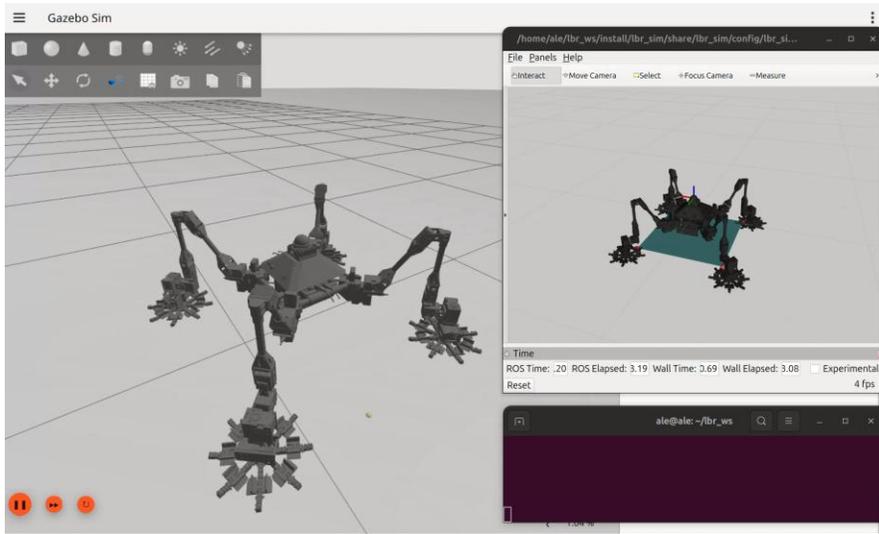


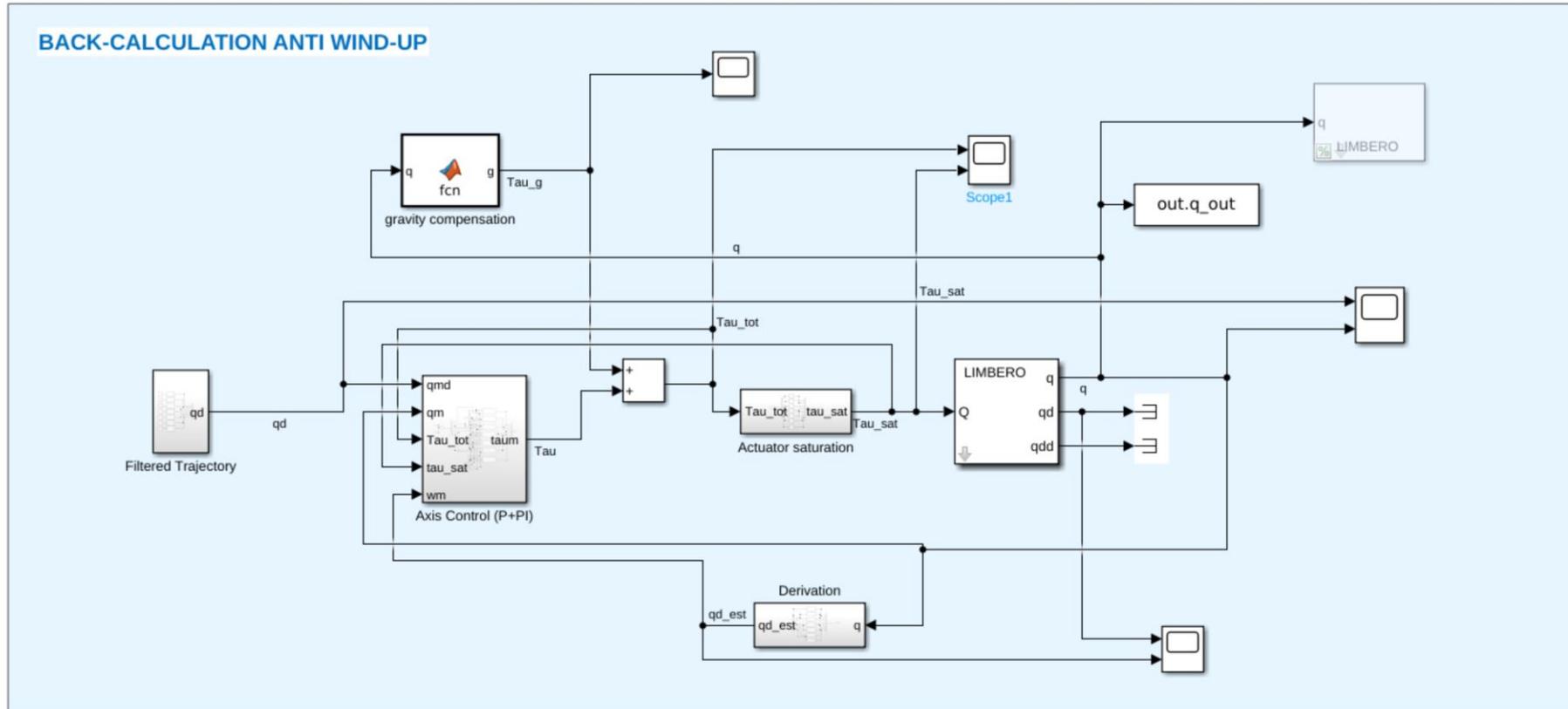


- ROS 2 components implementation
- Preliminary communication testing
- High-Level algorithms testing

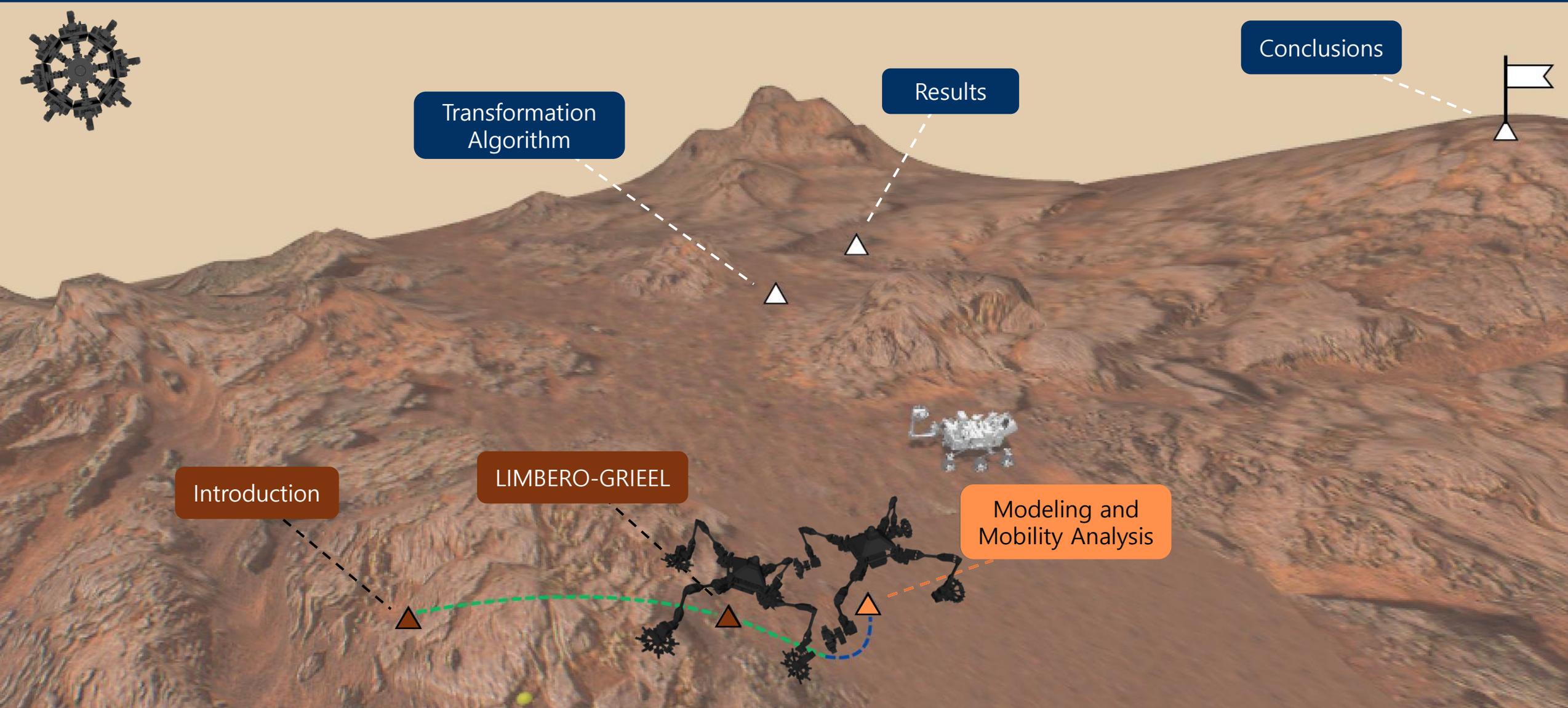


- Advanced motion testing
- Improve sim-to-real reliability
- New joint-controllers implementation





- Joint-controllers design and tuning
- Approximated Single limb simulation



Introduction

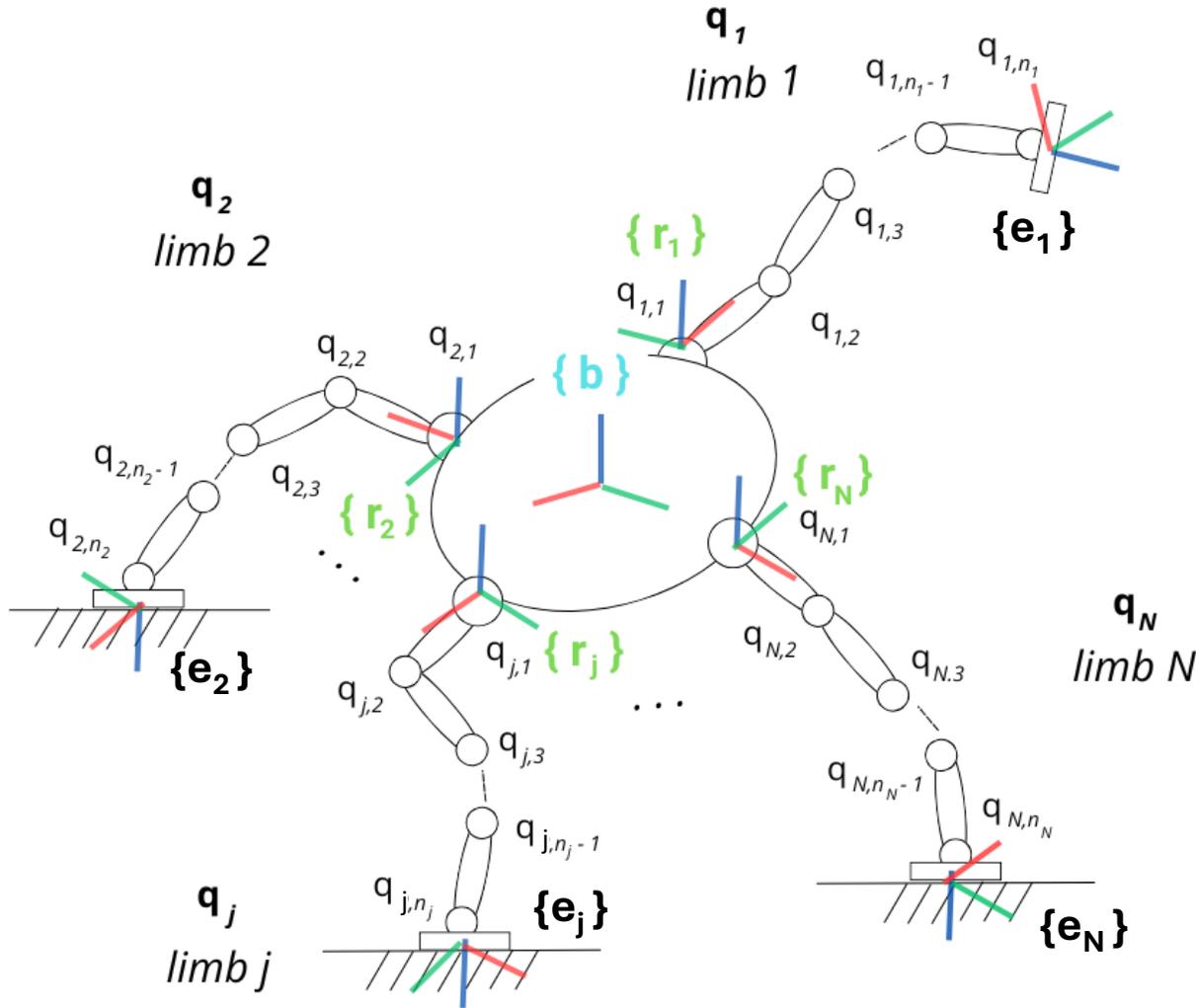
LIMBERO-GRIEEL

Transformation Algorithm

Results

Conclusions

Modeling and Mobility Analysis



## Symbols

$j \in J = \{1, \dots, N\}, \quad J_c \subseteq J, \quad N_c = |J_c|, \quad \mathbf{b}, \quad \mathbf{e}_j, \quad \mathbf{r}_j$

$\mathbf{q}_j \in \mathbb{R}^{n_j} \quad \mathbf{q} = [\mathbf{q}_1 \ \dots \ \mathbf{q}_N]^T \in \mathbb{R}^n, \quad n = \sum_j n_j$

$$\mathbf{T}_f^0(\mathbf{q}) = \begin{bmatrix} \mathbf{R}_f^0(\mathbf{q}) & {}^0\mathbf{p}_f(\mathbf{q}) \\ \mathbf{0}^T & 1 \end{bmatrix}$$

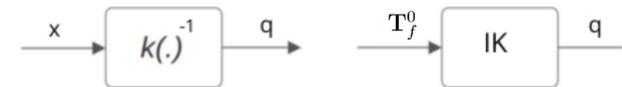
## Forward Kinematics

$\mathbf{x} = k(\mathbf{q}) \in \mathbb{R}^m$



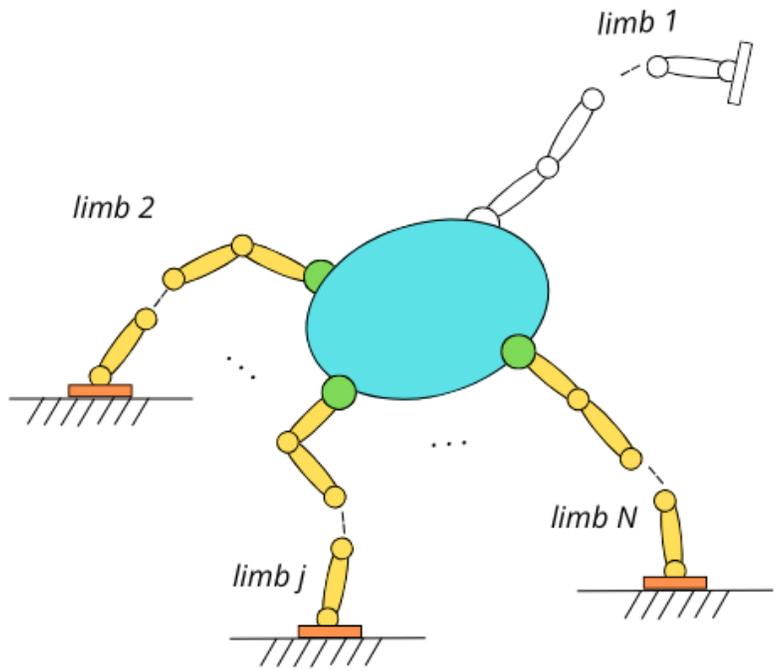
$$\mathbf{T}_{e_j}^b(\mathbf{q}_j) = \mathbf{T}_{r_j}^b \cdot \mathbf{T}_{j_0}^r \cdot \mathbf{T}_{j_1}^{j_0}(\mathbf{q}_{j,1}) \cdots \mathbf{T}_{j_i}^{j_{i-1}}(\mathbf{q}_{j,i}) \cdots \mathbf{T}_{j_{n_j-1}}^{j_{n_j-2}}(\mathbf{q}_{j,n_j-1}) \cdot \mathbf{T}_{e_j}^{j_{n_j-1}}, \forall j = 1, \dots, N$$

## Inverse Kinematics



# Kinematic Model: Multiarm parallelism

Limbed Robot



$N_c$  contact limbs

- Limb
- Limb root
- Limb end
- Base

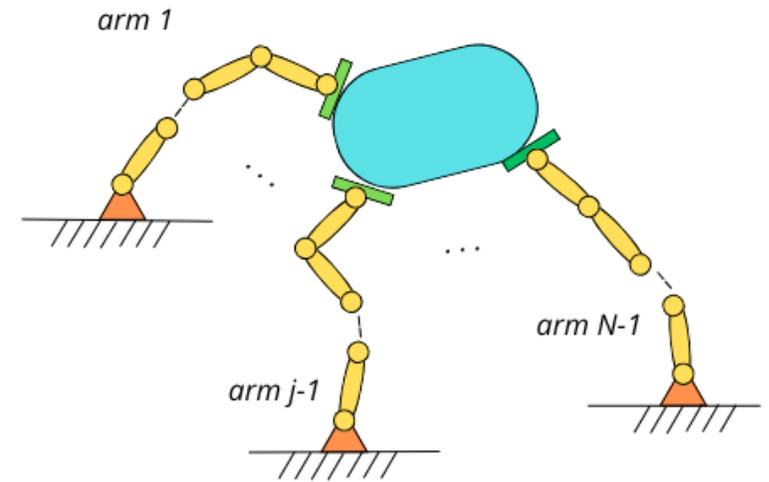
## Assumptions

- Rigid gripper-ground contact
- Tight grasp

## Multilimb-Multiarm duality

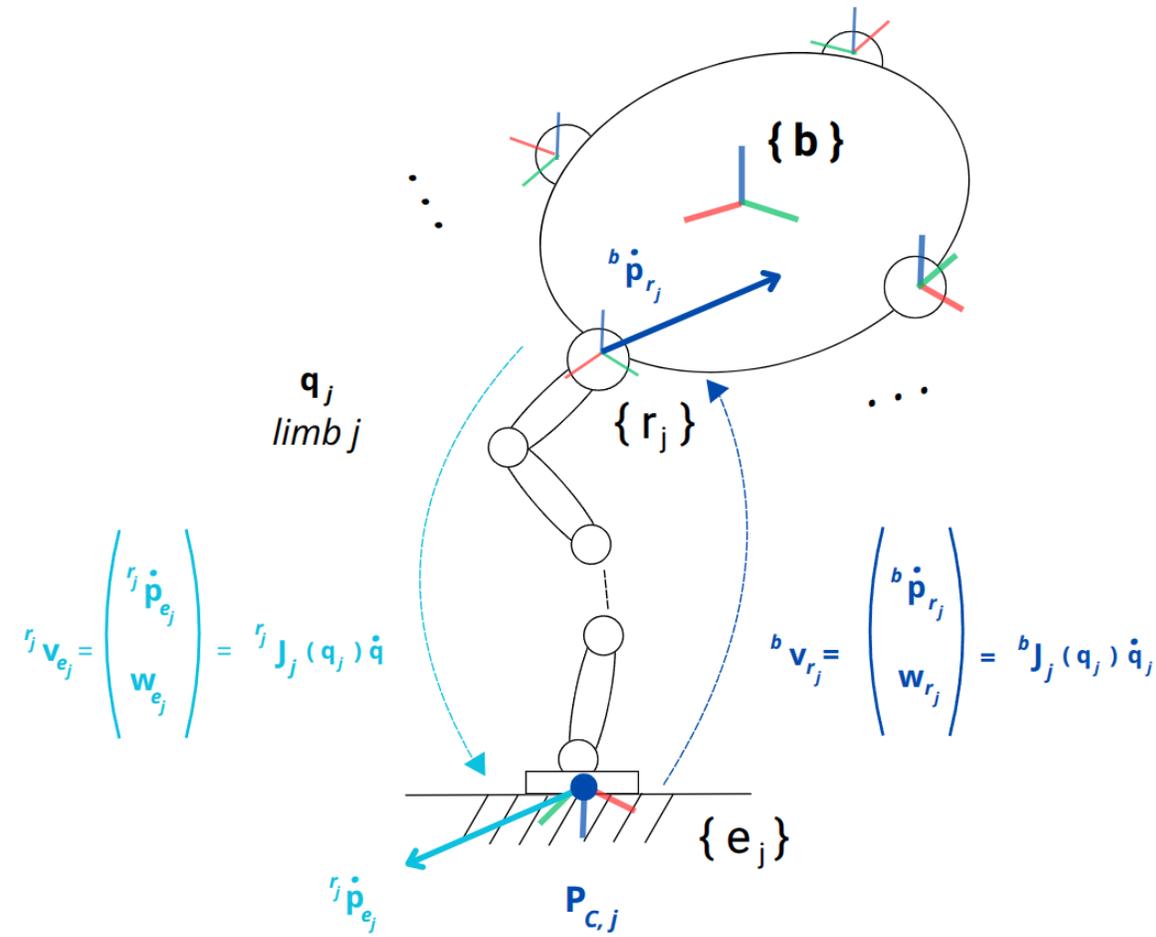


Cooperative Manipulators



$N_c$  cooperating arms

- Arm
- Arm EE
- Arm base
- Object



## Symbols

$$\dot{q}_j \in \mathbb{R}^{n_j} \quad \dot{q} \in \mathbb{R}^n$$

$${}^h v_k \in \mathbb{R}^6 \quad {}^h J_k \in \mathbb{R}^{6 \times 6} \quad J_k^h \in \mathbb{R}^{6 \times 6}$$

## Velocity relation (assumptions)

$${}^e_j v_{r_j} = -{}^r_j v_{e_j}$$

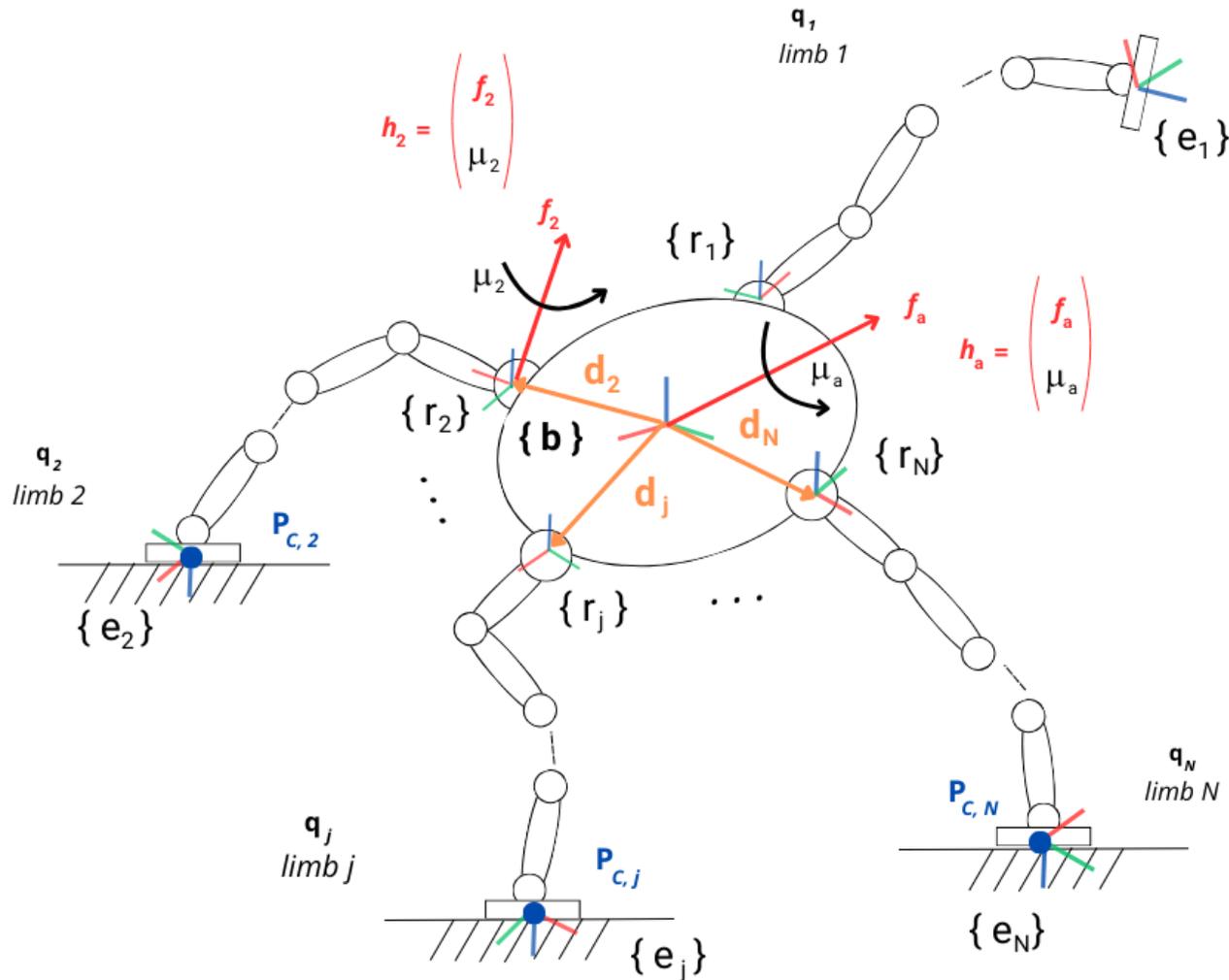
$${}^b v_{r_j} = -J_{r_j}^{b r_j} J_j(q_j) \cdot \dot{q}_j = {}^b J_j(q_j) \cdot \dot{q}_j$$

$$J_0^k = \begin{bmatrix} R_0^k & 0_{3 \times 3} \\ 0_{3 \times 3} & R_0^k \end{bmatrix}$$

## Differential Kinematics model

$${}^b J_j(q_j) = -J_{r_j}^{b r_j} J_j(q_j)$$

$$J(q) = \text{diag}({}^b J_1(q_1) \dots {}^b J_j(q_j) \dots {}^b J_N(q_N)), \quad J_j(q_j) = 0 \in \mathbb{R}^{m \times n_j} \quad \text{if } j \notin J_c$$



## Symbols

$$W \in \mathbb{R}^{m \times M} \quad h_a \in \mathbb{R}^m \quad v_a \in \mathbb{R}^m \quad h \in \mathbb{R}^M, M = m \cdot N_c$$

$$\tau \in \mathbb{R}^n$$

## Quantities definition

$$W = [W_1 \dots W_j \dots W_N], \quad \begin{cases} W_j = \mathbf{0} \in \mathbb{R}^{m \times m} & \text{if } j \notin J_c \\ W_j = \begin{bmatrix} \mathbf{I}_3 & \mathbf{0}_3 \\ \mathbf{R}_j & \mathbf{I}_3 \end{bmatrix}, & \text{if } j \in J_c \end{cases}$$

$$h_a = Wh$$

$$h = W^\dagger h_a$$

$$d_j \times f_j = R_j f_j$$

## Equations

$$J_a^T(q) = J^T(q)W^\dagger \in \mathbb{R}^{n \times m}$$

$$\tau = J_a^T(q)h_a$$

$$v_a = J_a(q)\dot{q}$$

### Absolute Base Manipulability Ellipsoid equations

$$\mathbf{E}_a \in \mathbb{R}^{m \times m}$$

$$\mathbf{h}_a^T [\mathbf{J}_a(\mathbf{q}) \mathbf{J}_a^T(\mathbf{q})] \mathbf{h}_a = 1$$

$$\mathbf{J}_a = \begin{bmatrix} \mathbf{J}_{P_a} \\ \mathbf{J}_{O_a} \end{bmatrix}$$

$$\mathbf{E}_a = \begin{bmatrix} \mathbf{E}_{T_a} & \mathbf{E}_{TR_a} \\ \mathbf{E}_{TR_a}^T & \mathbf{E}_{R_a} \end{bmatrix}$$

$$\dot{\mathbf{p}}_a^T [\mathbf{E}_{T_a}]^{-1} \dot{\mathbf{p}}_a = 1$$

Absolute Translational Base Velocity Manipulability Ellipsoid (ATBVME)

$$\boldsymbol{\omega}_a^T [\mathbf{E}_{R_a}]^{-1} \boldsymbol{\omega}_a = 1$$

Absolute Rotational Base Velocity Manipulability Ellipsoid (ARBVME)

$$\mathbf{v}_a^T [\mathbf{J}_a(\mathbf{q}) \mathbf{J}_a^T(\mathbf{q})]^{-1} \mathbf{v}_a = 1$$

### Velocity scaling

$$\dot{\mathbf{q}}_{lim,j} = \begin{bmatrix} \dot{q}_{lim,1} & \dot{q}_{lim,2} & \dots & \dot{q}_{lim,n_j} \end{bmatrix}^T$$

$$\mathbf{Q}_{lim} = \text{diag} \left( \begin{bmatrix} \dot{q}_{lim,1} & \dot{q}_{lim,2} & \dots & \dot{q}_{lim,N} \end{bmatrix} \right)$$

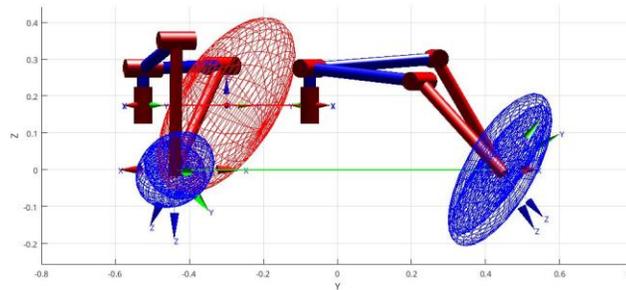
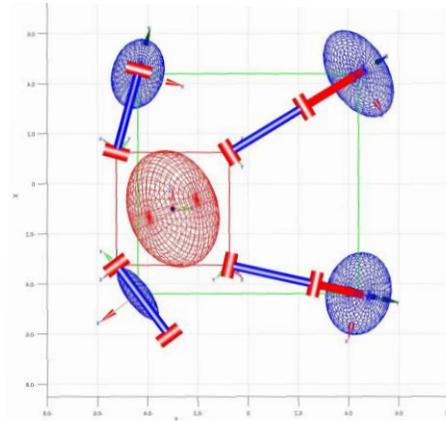
$$\tilde{\mathbf{q}} = \mathbf{Q}_{lim}^{-1} \dot{\mathbf{q}}$$

$$\tilde{\mathbf{q}}^T \tilde{\mathbf{q}} = 1$$

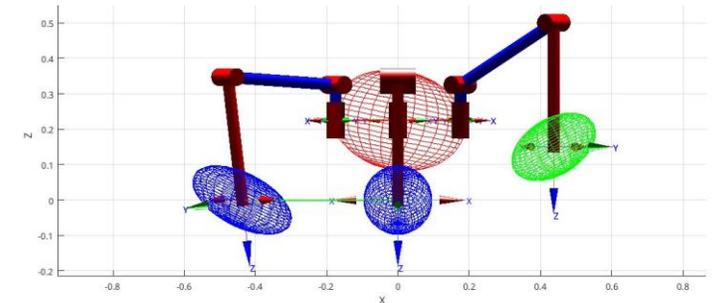
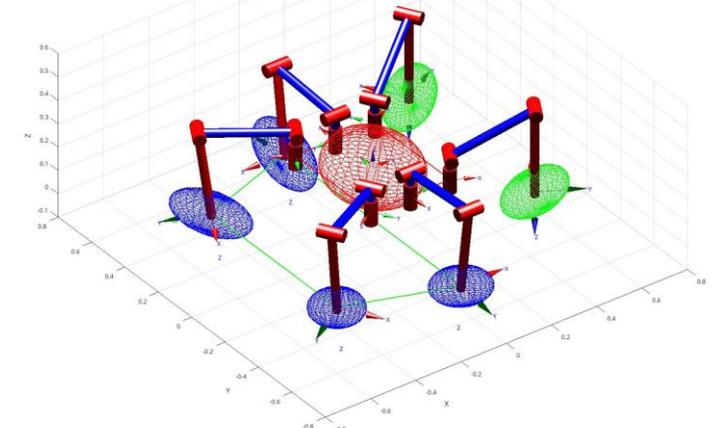
$$\tilde{\mathbf{J}}(\mathbf{q}) = \mathbf{J}(\mathbf{q}) \cdot \mathbf{Q}_{lim}$$

$$\tilde{\mathbf{J}}_a^T(\mathbf{q}) = \tilde{\mathbf{J}}^T(\mathbf{q}) \mathbf{W}^\dagger \in \mathbb{R}^{n \times m}$$

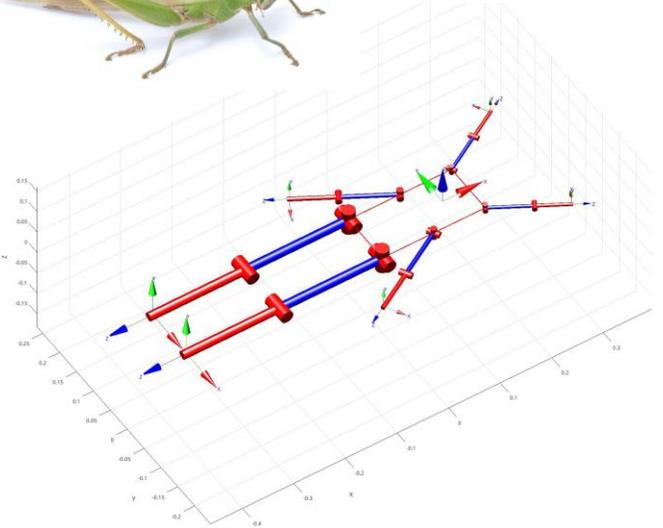
4-limbed



6-limbed

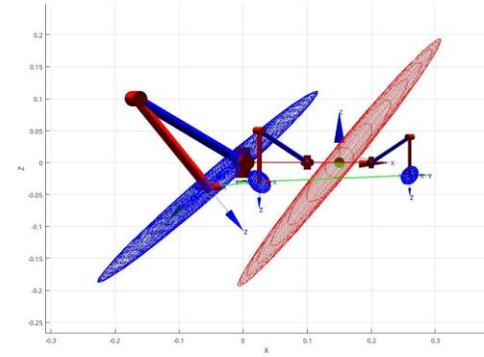
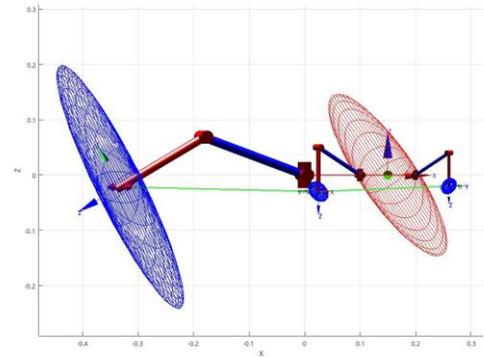


# Manipulability Analysis: Bioinspired Example

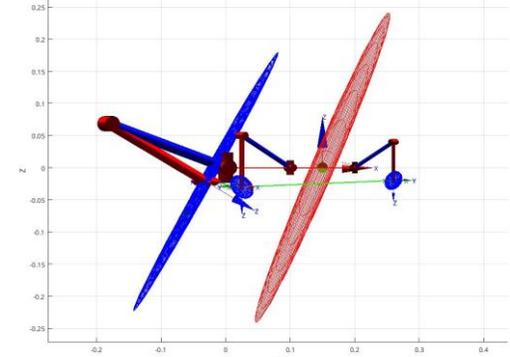


**Jumping:** sensitivity to rear legs configuration  $|q_{LB/RB,1}| = 15^\circ$

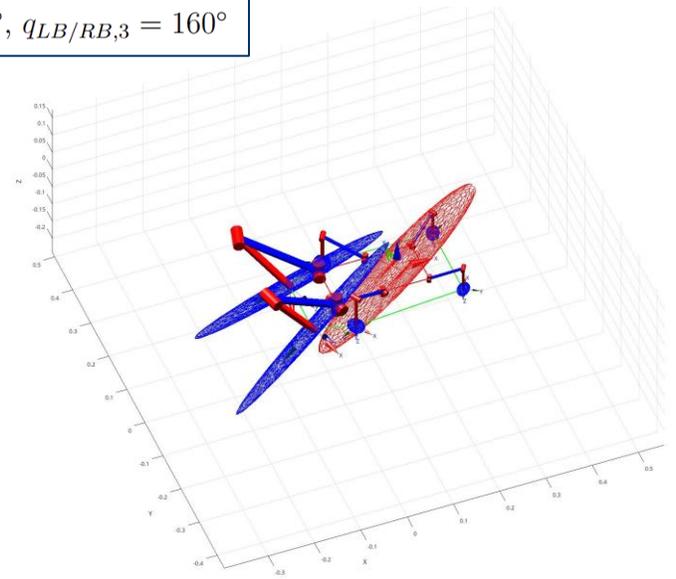
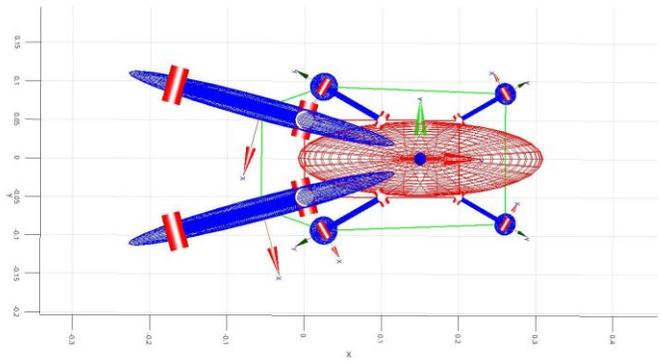
$$q_{LB/RB,2} = -20^\circ, q_{LB/RB,3} = 50^\circ$$



$$q_{LB/RB,2} = -30^\circ, q_{LB/RB,3} = 170^\circ$$



$$q_{LB/RB,2} = -30^\circ, q_{LB/RB,3} = 160^\circ$$



## Configuration and Limits

$$\mathbf{q} = [q_{LF} \ q_{LM} \ q_{LB} \ q_{RF} \ q_{RM} \ q_{RB}]^T \in \mathbb{R}^{18}$$

$$\dot{q}_{lim,LF/RF} = [0.8 \ 0.8 \ 0.8]$$

$$\dot{q}_{lim,LM/RM} = [0.8 \ 0.8 \ 0.8]$$

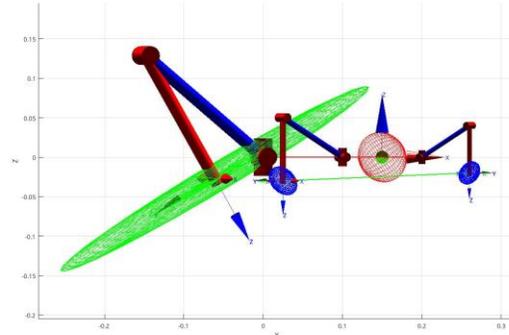
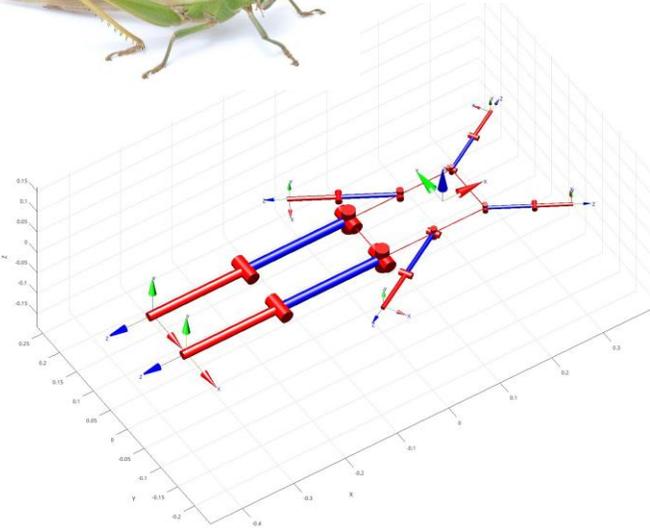
$$\dot{q}_{lim,LB/RB} = [1.0 \ 1.0 \ 4.0]$$

# Manipulability Analysis: Bioinspired Example

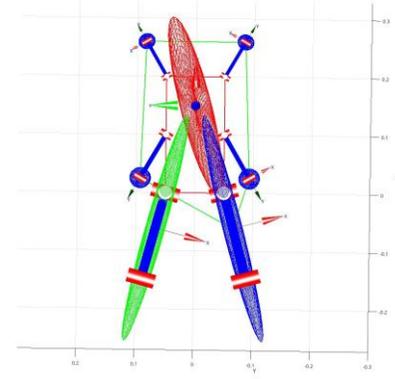


**Jumping:** sensitivity to rear legs availability and orientation

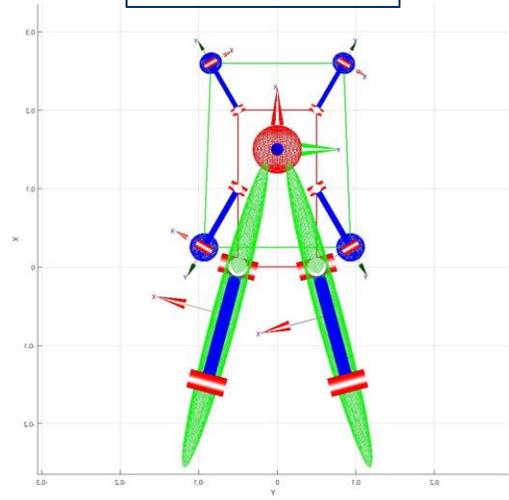
$$|q_{LB/RB,1}| = 15^\circ \quad q_{LB/RB,2} = -30^\circ, \quad q_{LB/RB,3} = 160^\circ$$



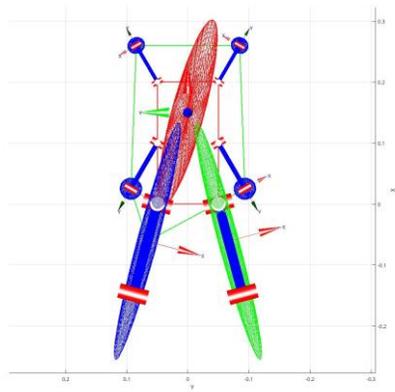
NOT LB



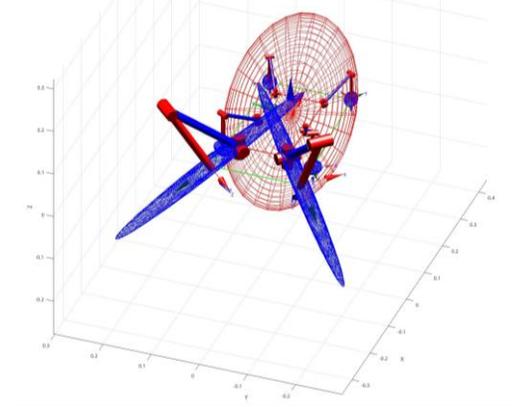
NOT LB and RB



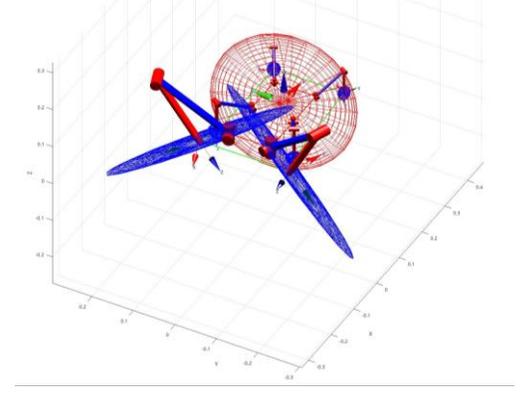
NOT RB



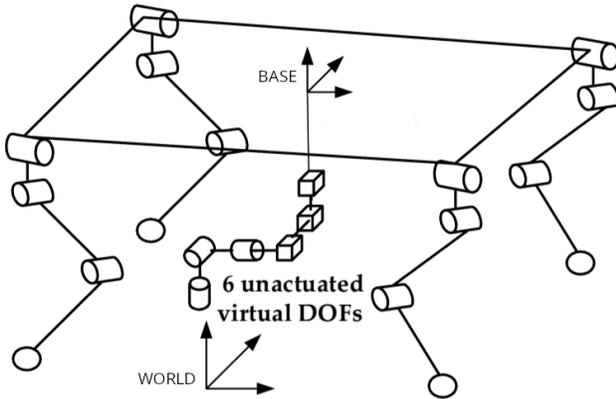
$|q_{LB/RB,1}| = 45^\circ$



$|q_{LB/RB,1}| = 70^\circ$



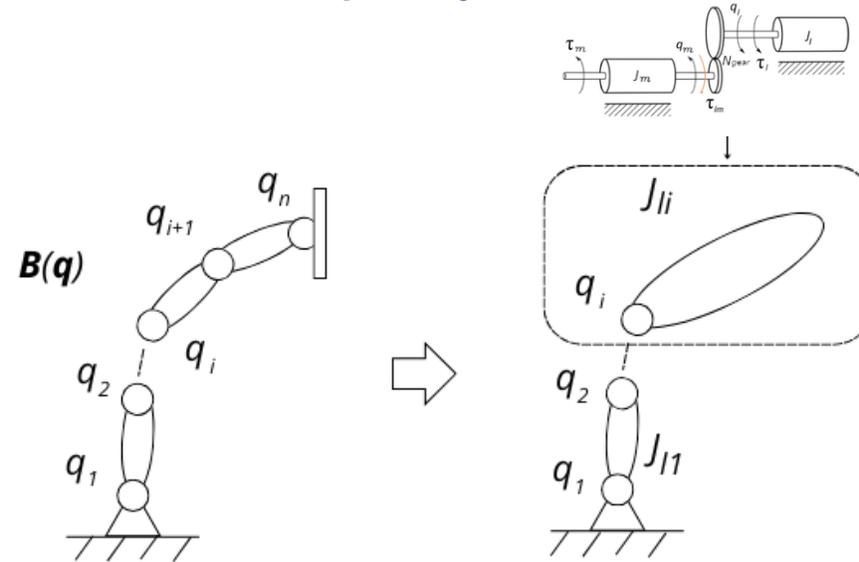
### Floating Base Dynamics



$$\mathbf{q} = [\mathbf{q}_b \quad \mathbf{q}_1 \quad \mathbf{q}_2 \quad \dots \quad \mathbf{q}_N]^T \quad \mathbf{q} \in \mathbb{R}^{n+6}, (n = \sum_j n_j)$$

$$\begin{cases} \mathbf{B}(\mathbf{q})\ddot{\mathbf{q}} + \mathbf{C}(\mathbf{q}, \dot{\mathbf{q}})\dot{\mathbf{q}} + \mathbf{g}(\mathbf{q}) = \mathbf{J}_M^T(\mathbf{q})\boldsymbol{\tau} - \mathbf{J}_C^T(\mathbf{q})\mathbf{h}_c \\ \mathbf{J}_c\ddot{\mathbf{q}} + \dot{\mathbf{J}}_c\dot{\mathbf{q}} = 0 \end{cases}$$

### Decoupled Dynamics



$$\left( J_{mi} + \frac{J_{li}}{N_{gear,i}^2} \right) \ddot{q}_{mi} = \tau_{mi} - \frac{\tau_{di}}{N_{gear,i}} \quad i = 1, \dots, n$$

$$\tau_{di} = \sum_{j \neq i} C_{ij}(\mathbf{q}) \cdot \dot{q}_j^2 + \sum_{j \neq i} B_{ij}(\mathbf{q}) \cdot \ddot{q}_j + g_i(\mathbf{q})$$

# Modeling and Mobility Analysis

## LIMBERO-GRIEEL Model

$$j \in J = \{1, 2, 3, 4\}, \quad J_c \subseteq J$$

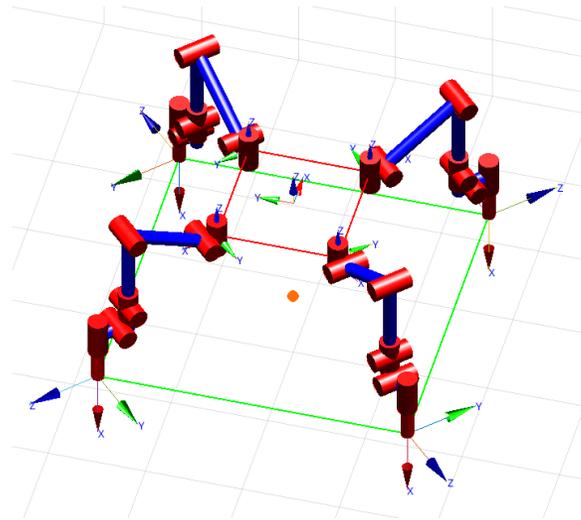
$$N = |J| = 4, \quad N_c = |J_c|$$

$$n_j = 7, \quad n = n_j \cdot N = 28$$

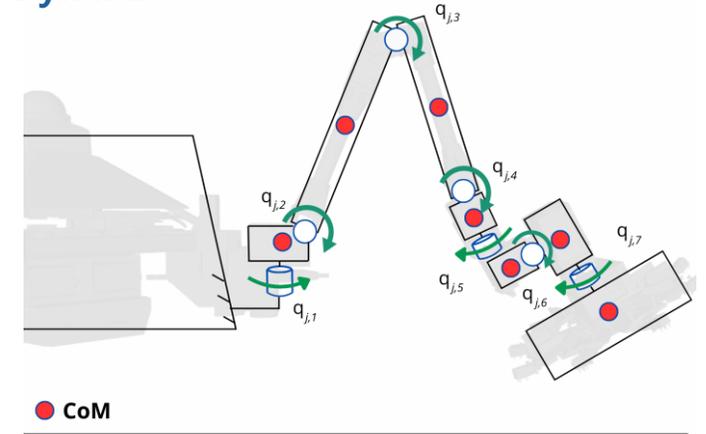
$$\mathbf{q}_j = [q_{j,1} \ q_{j,2} \ q_{j,3} \ q_{j,4} \ q_{j,5} \ q_{j,6} \ q_{j,7}]^T \in \mathbb{R}^7$$

$$\mathbf{q} = [\mathbf{q}_1 \ \mathbf{q}_2 \ \mathbf{q}_3 \ \mathbf{q}_4]^T \in \mathbb{R}^{28}$$

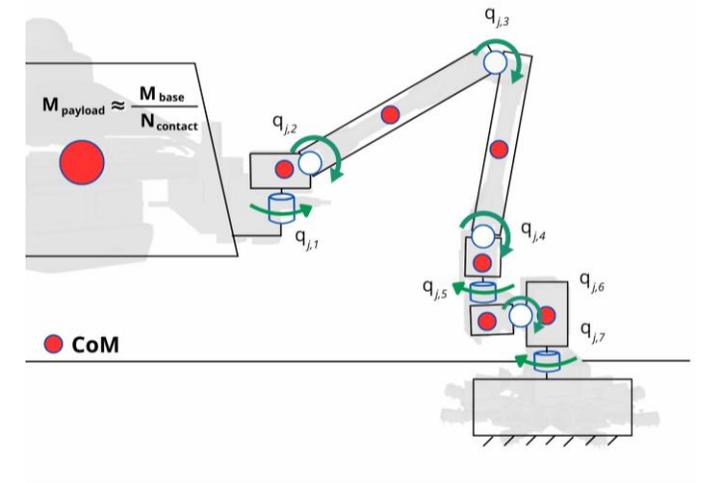
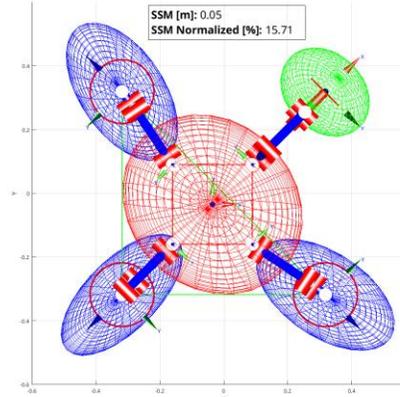
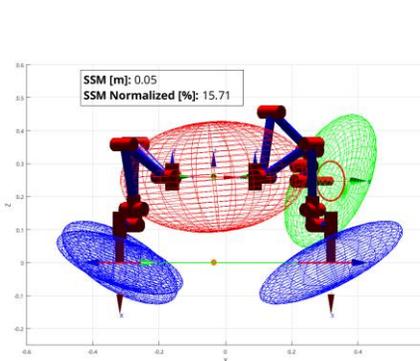
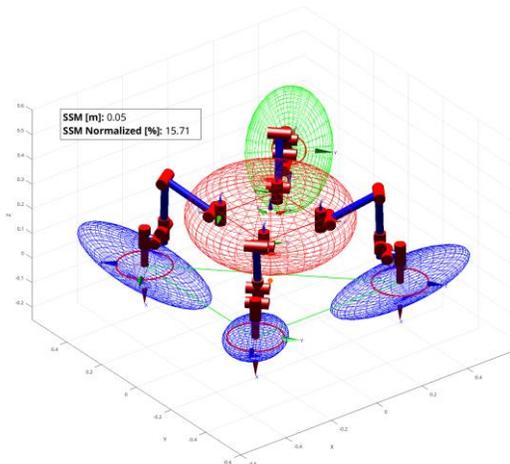
### Kinematics

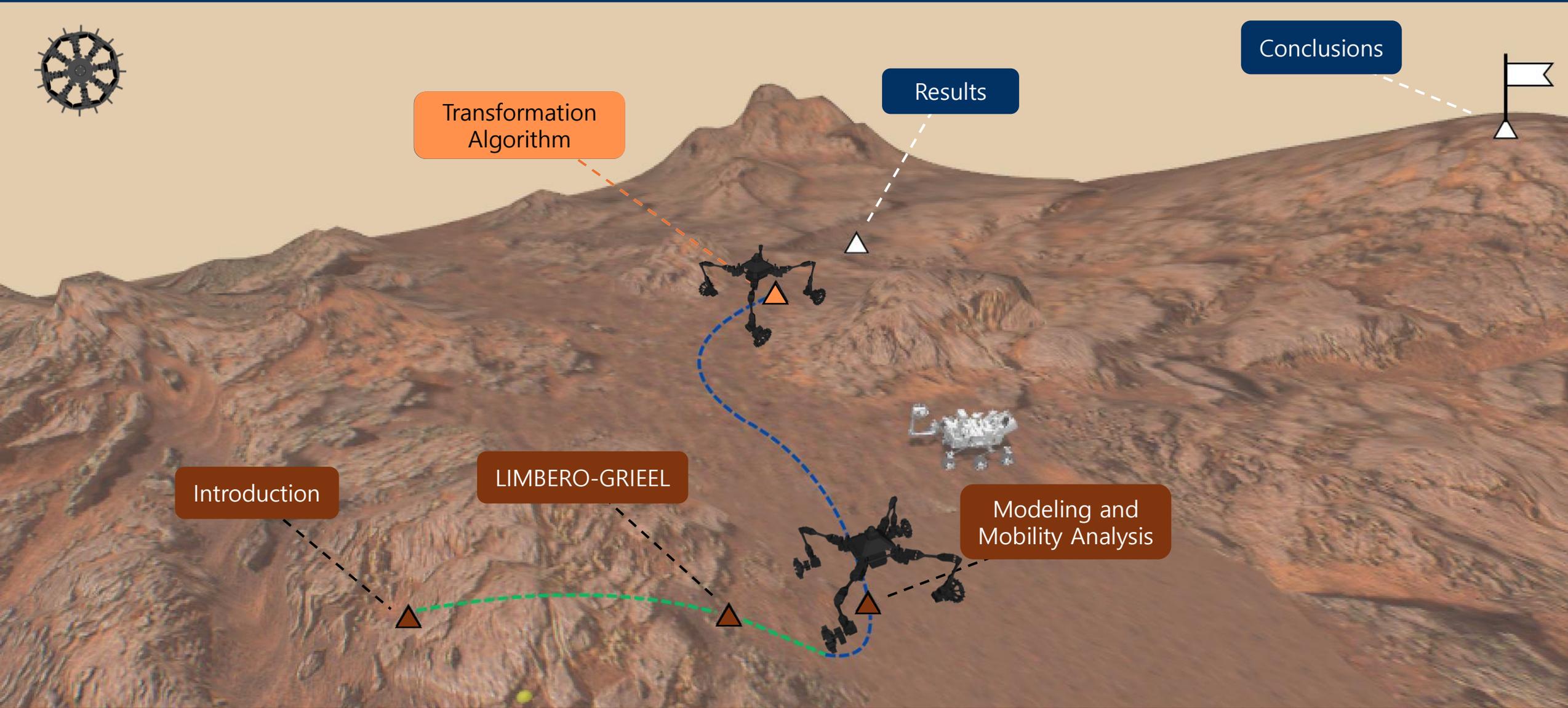


### Dynamics



### Manipulability





Introduction

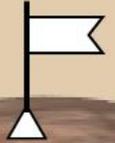
LIMBERO-GRIEEL

Transformation  
Algorithm

Results

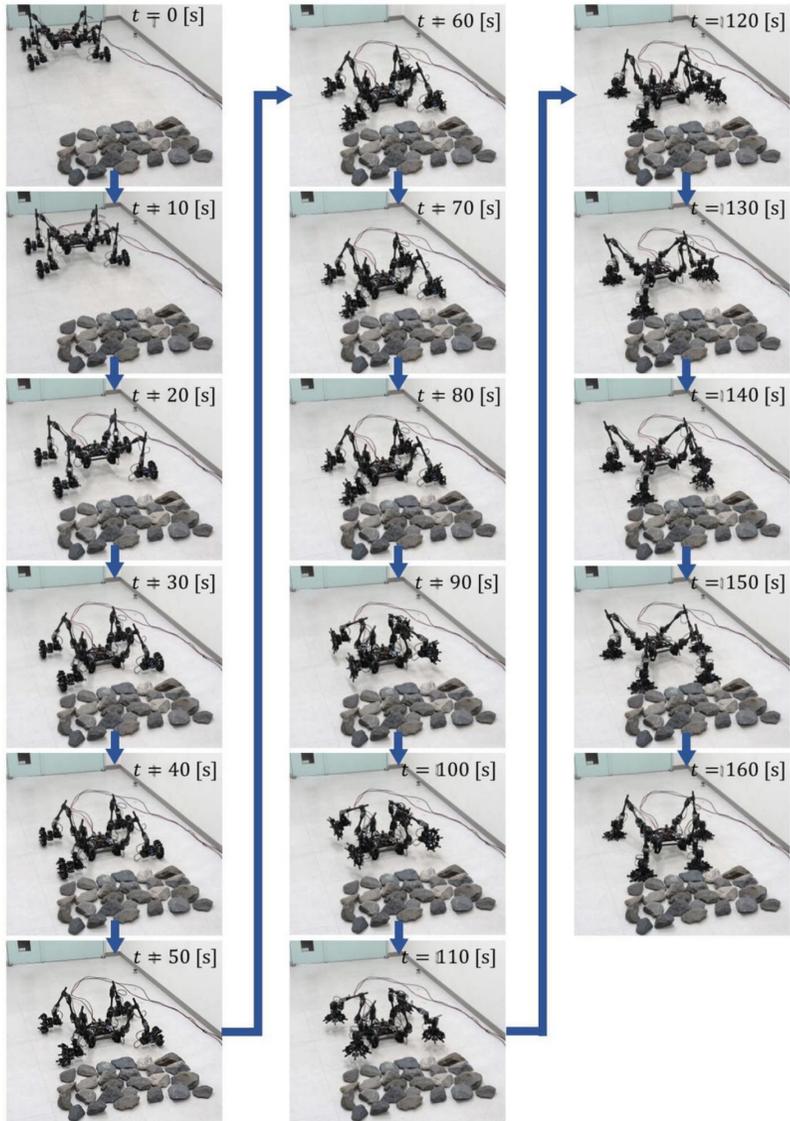
Modeling and  
Mobility Analysis

Conclusions



# Transformation Algorithm

## Previous Sequence



- Quick and simple
- Always stable **in flat terrains**



- Not flexible
- Base wear in rough terrains
- Not stable in **generic terrains**

### Improvement ideas

- Hold the base above the ground
- Transform limb-ends singularly

## Support polygon

$$SP = \text{Conv}(J_c) = \left\{ \sum_{j \in J_c} \lambda_j \mathbf{P}_{c,j} \mid \sum_{j \in J_c} \lambda_j = 1, \lambda_j \geq 0, \forall j \in J_c \right\}$$

$$\sigma_{SS}(\bar{\mathbf{P}}_{CoM}) = \begin{cases} +1 & \text{if } \exists \lambda_j \geq 0, j \in J_c \mid \sum_{j \in J_c} \lambda_j = 1, \bar{\mathbf{P}}_{CoM} = \sum_{j \in J_c} \lambda_j \mathbf{P}_{c,j} \\ -1 & \text{otherwise} \end{cases}$$

## Static stability (SS) criterion

*A legged locomotion machine supported by a stationary horizontal plane surface is statically stable at time  $t$  if and only if the vertical projection of the center of gravity of the machine onto the supporting surface lies within its support pattern at the given time*

$$SSM \geq 0$$

## Static Stability Margin

$$SSM = \sigma_{SS}(\bar{\mathbf{P}}_{CoM}) \cdot \min_j \frac{|(\mathbf{P}_{c,j+1} - \mathbf{P}_{c,j}) \times (\mathbf{P}_{c,j} - \bar{\mathbf{P}}_{CoM})|}{\|\mathbf{P}_{c,j+1} - \mathbf{P}_{c,j}\|}$$

$$SSM_{\%} = \frac{SSM}{SSM_{max}} \cdot 100$$

## Limitations and alternatives

- sloped terrains and relevant dynamics
- Zero Moment Point (ZMP),  
Tumble Stability (TS),  
Gravito Inertia Acceleration (GIA)

## Assumption

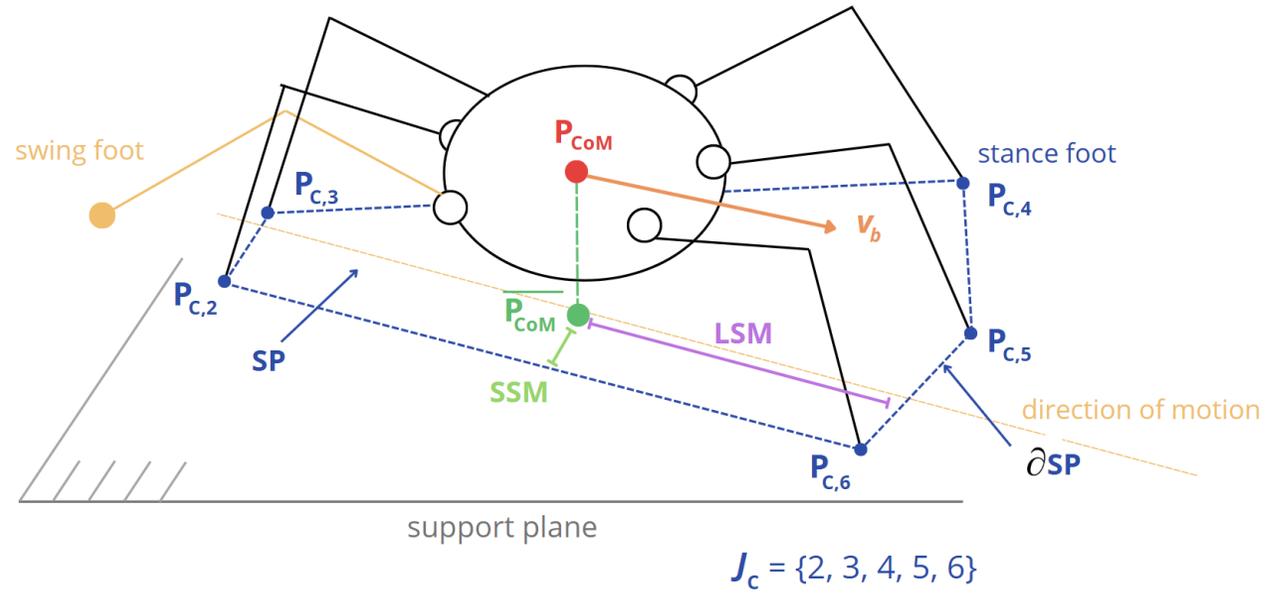
The locomotion mode transition occurs in approximately flat terrains, with quasi static motion

# Transformation Algorithm

## Multilimbed Robots Stability

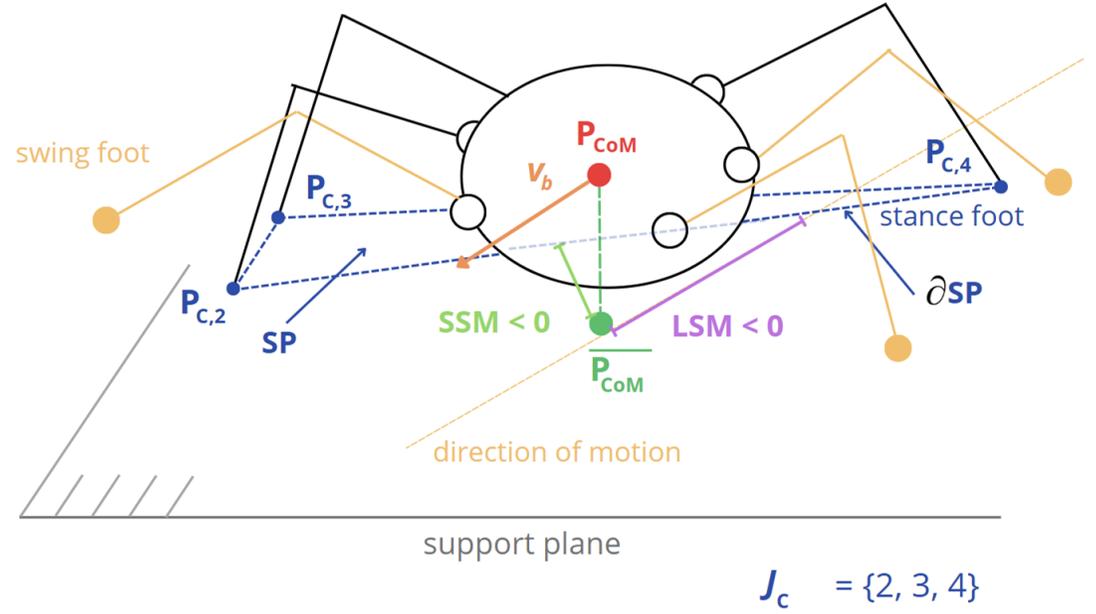
Stable

$$SSM \geq 0$$



Unstable

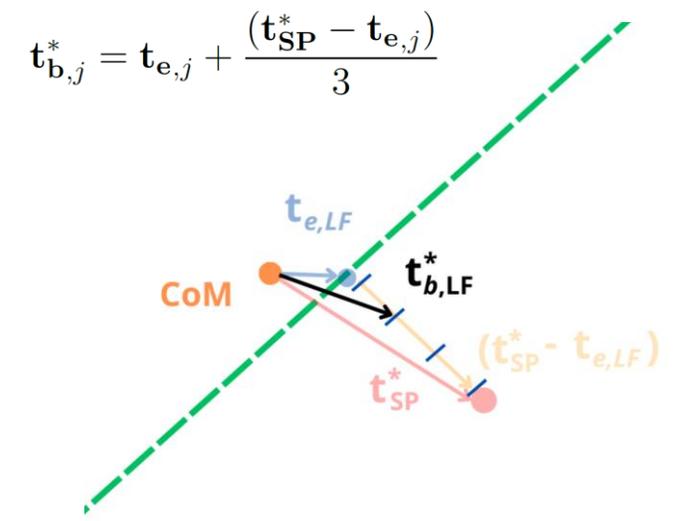
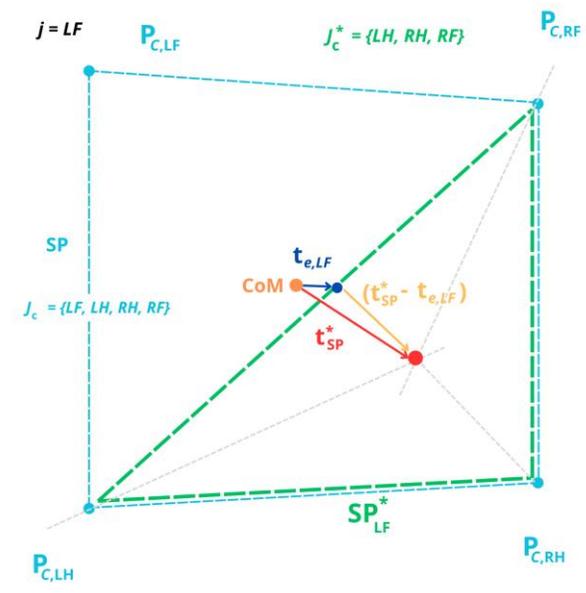
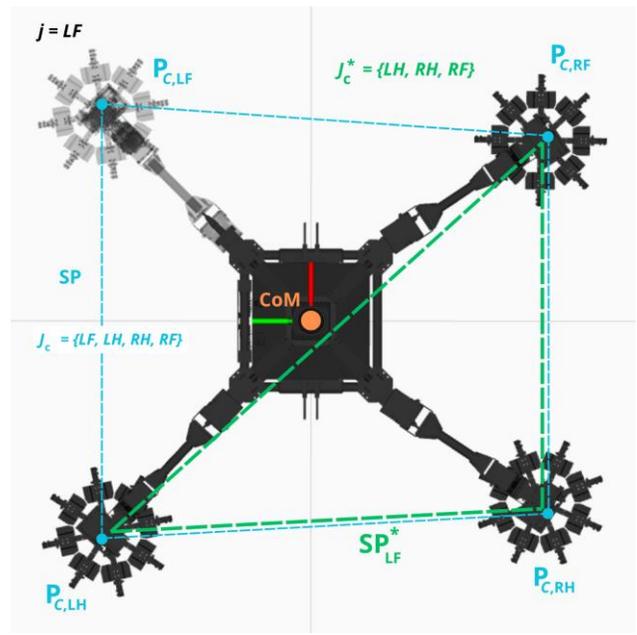
$$SSM < 0$$



# Proposed Sequence: Single Transformation

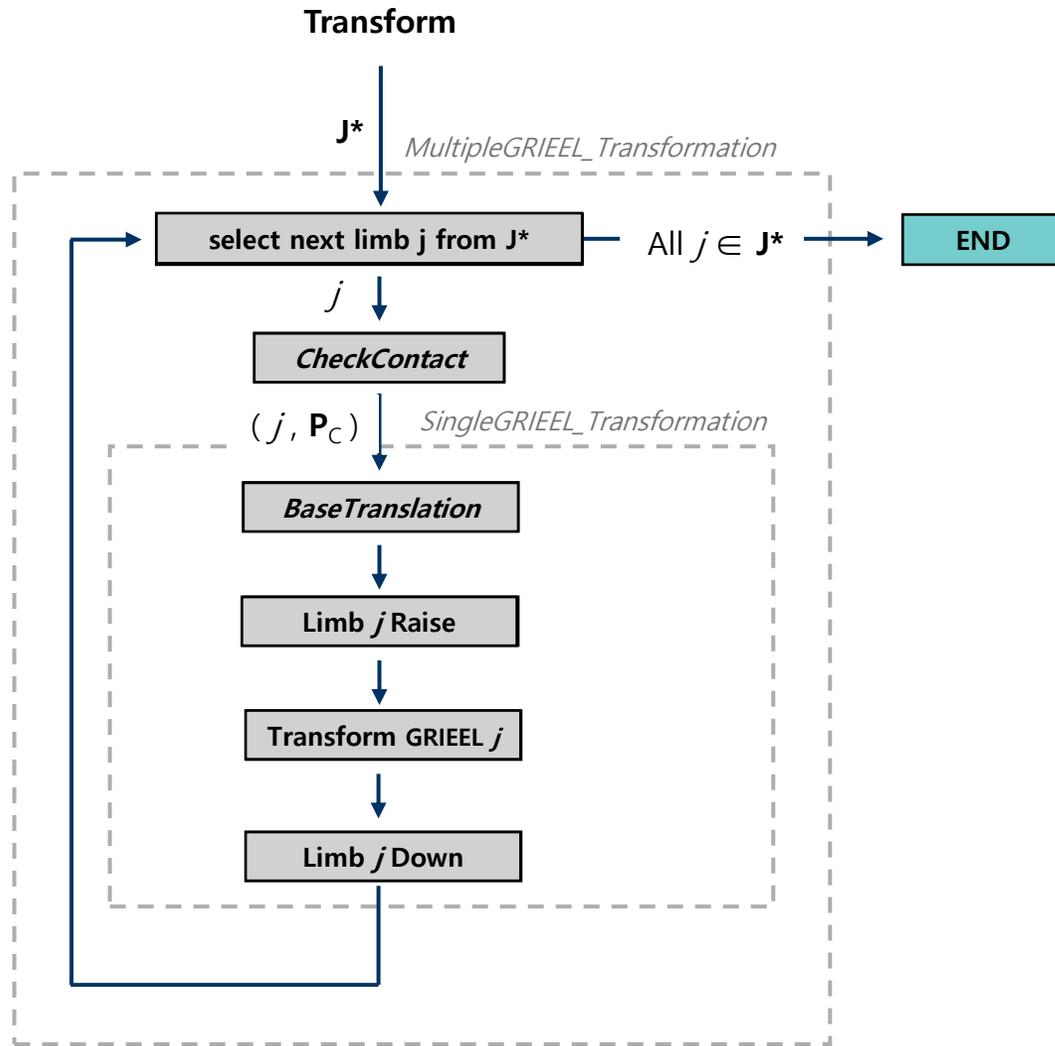
## Transformation idea: Anticipative base translation

1. Consider the next limb to transform (raised)
2. Move the base to keep Static Stability during the upcoming motion tasks
3. Perform transformation motion tasks

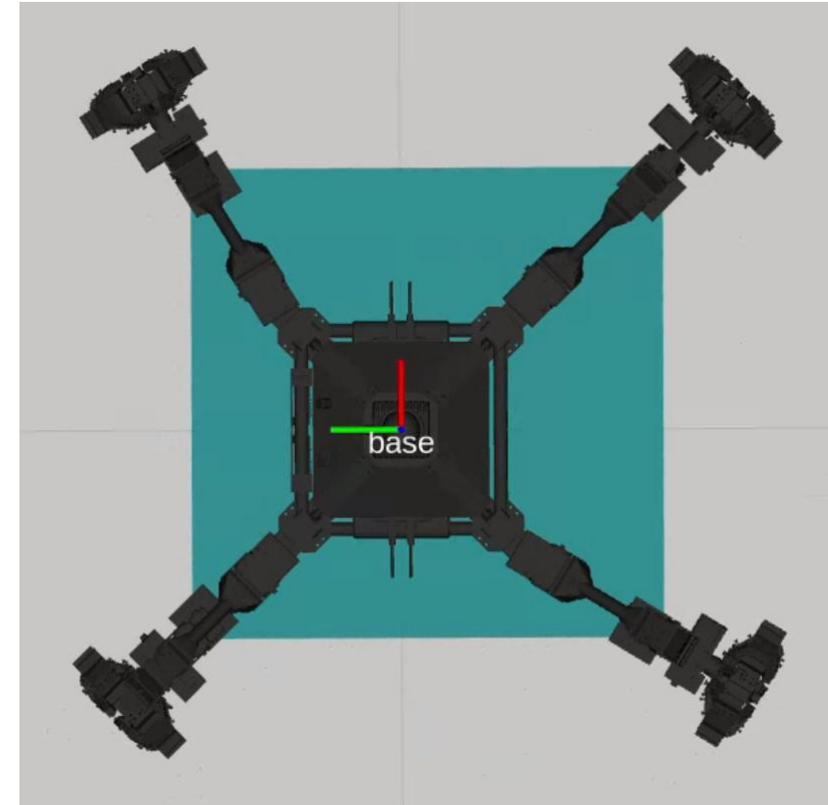


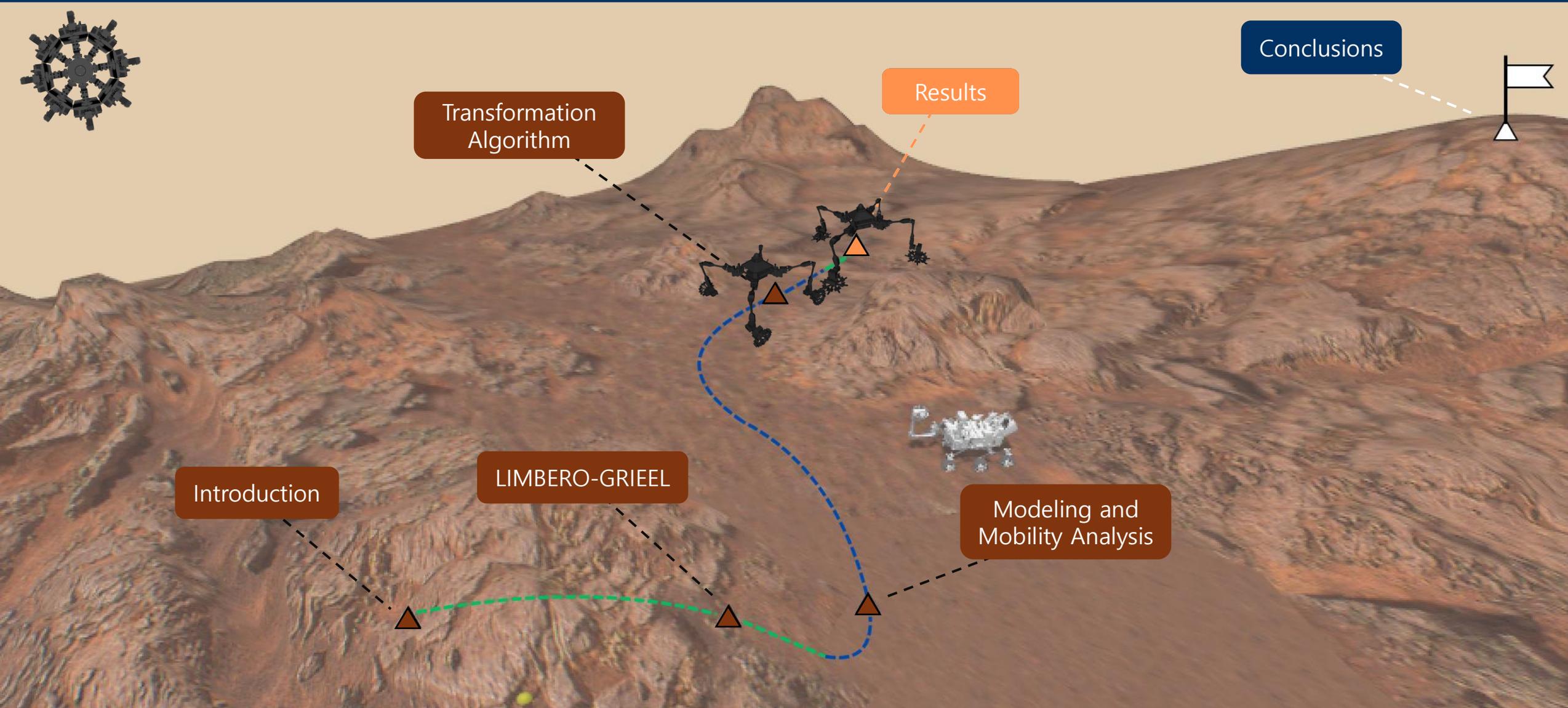
$$t_{b,j}^* = t_{e,j} + \frac{(t_{SP}^* - t_{e,j})}{3}$$

# Proposed Sequence: Algorithm



## WHEEL MODE





Transformation Algorithm

Results

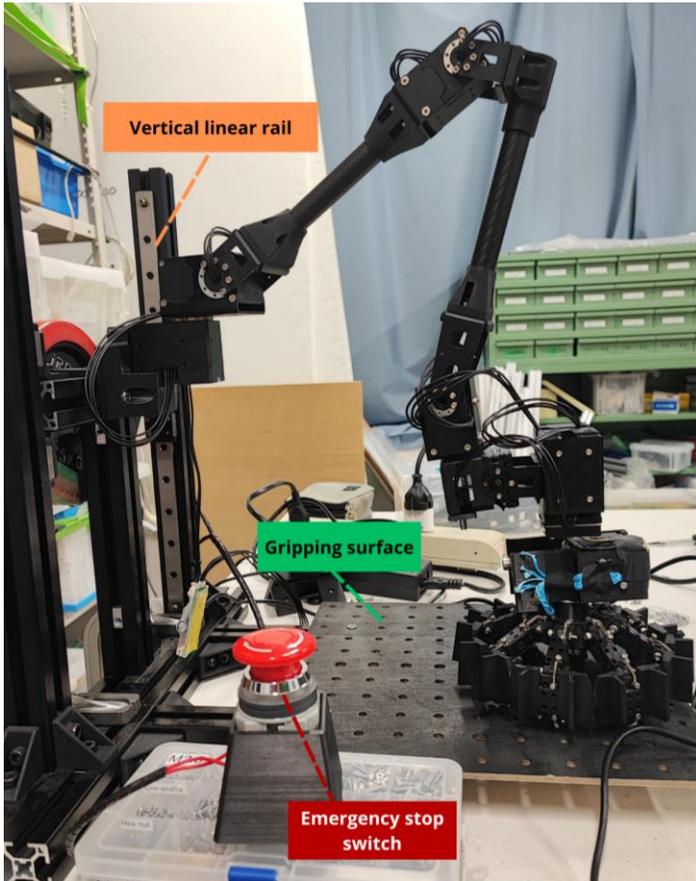
Conclusions

Introduction

LIMBERO-GRIEEL

Modeling and Mobility Analysis

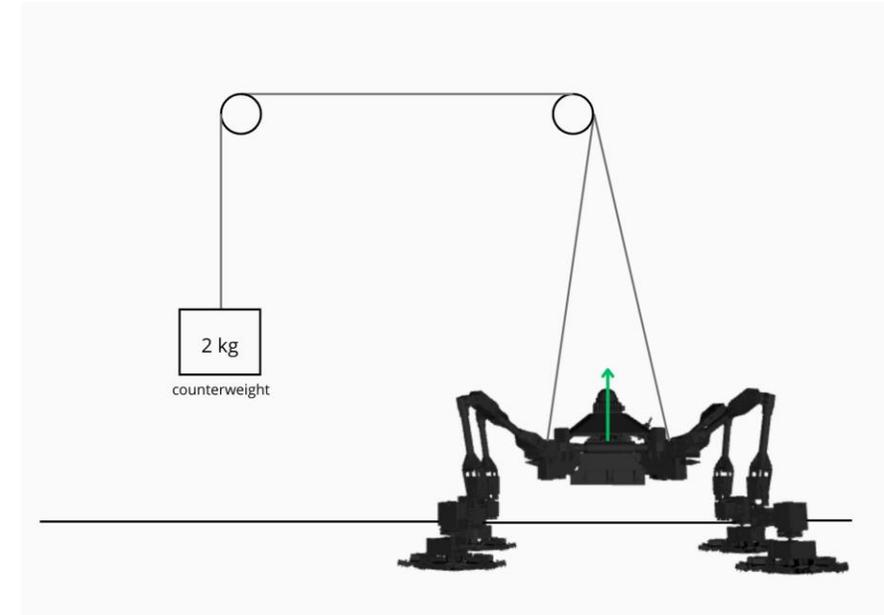
Single Limb Test

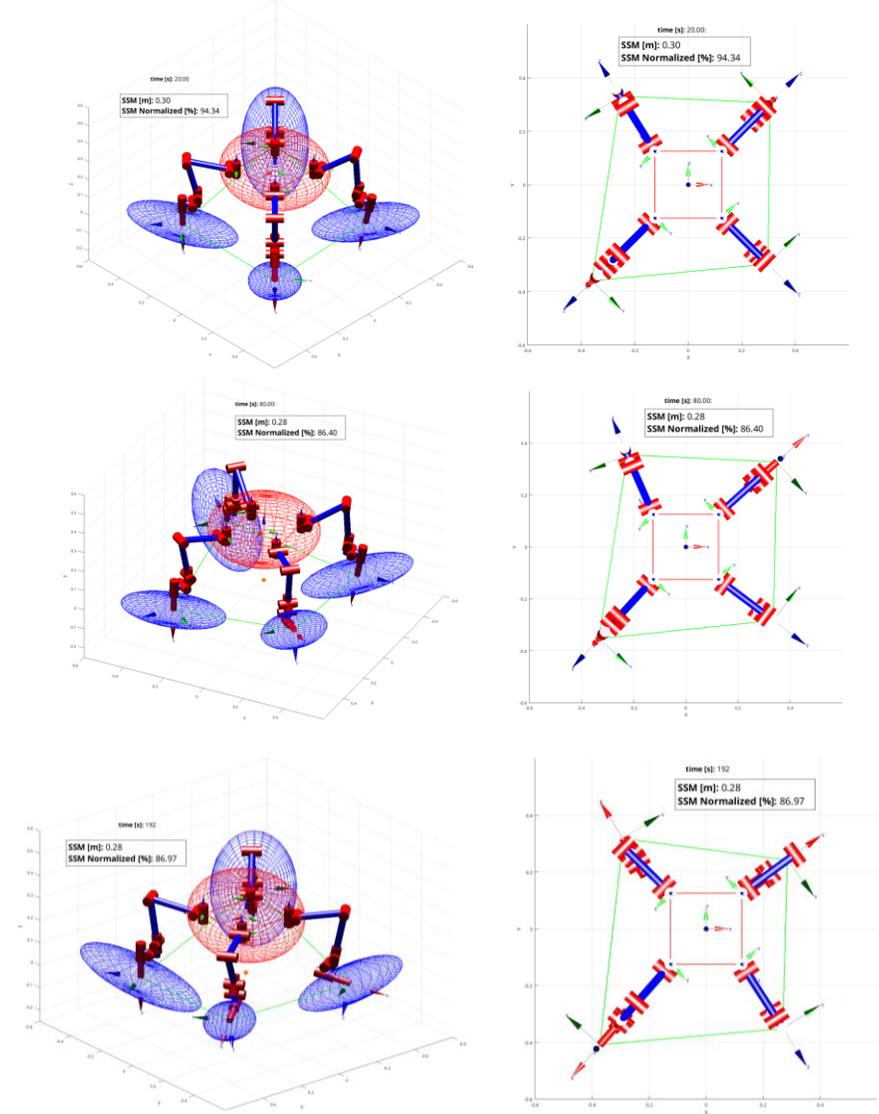
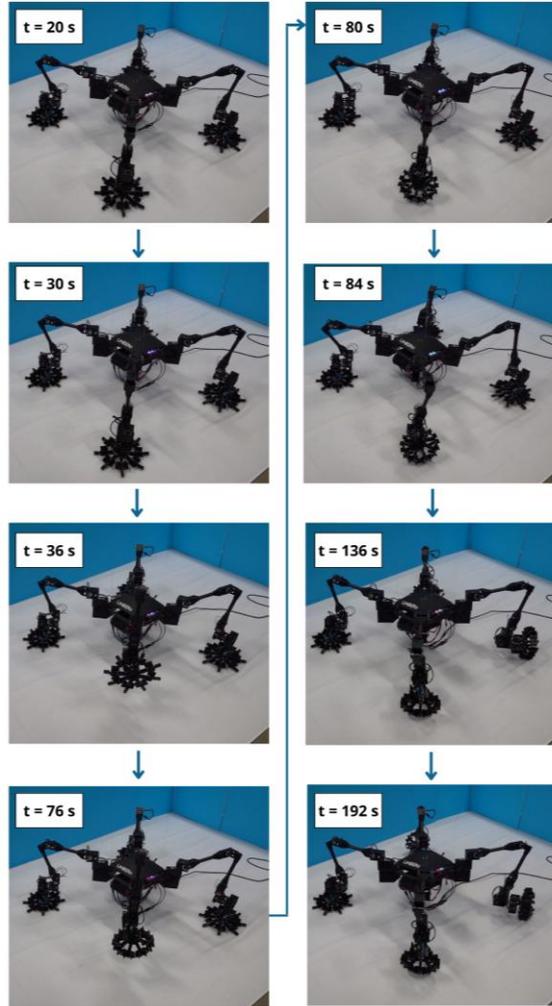


Robot Test

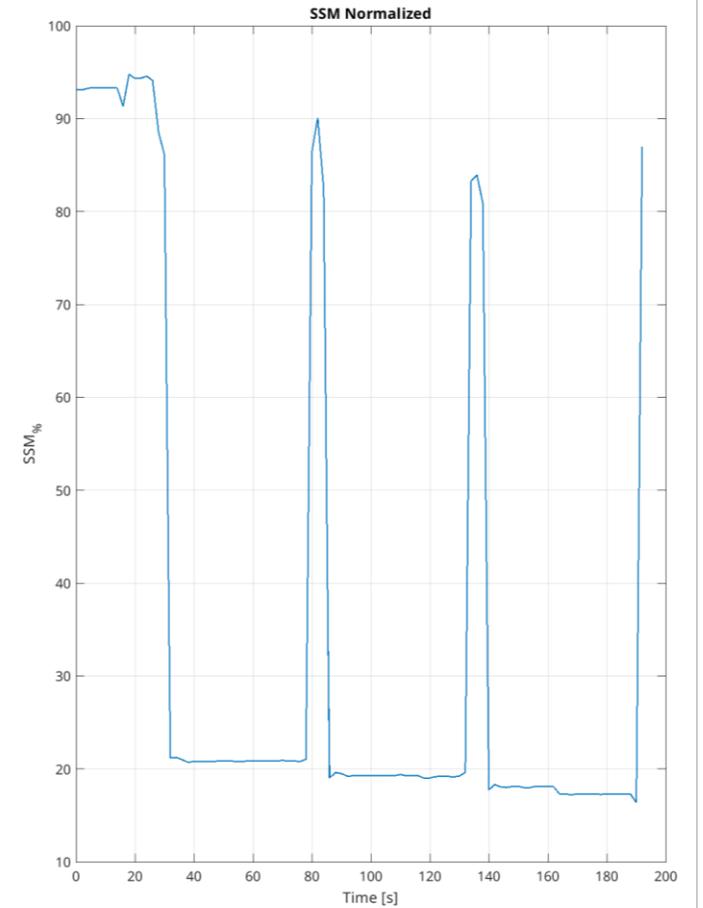
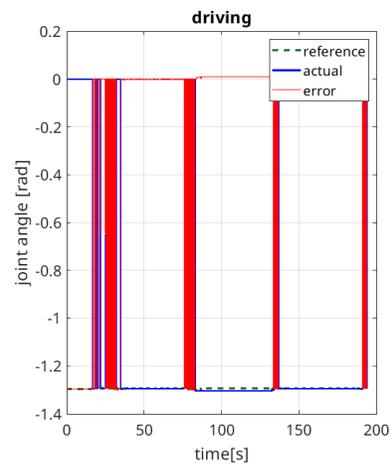
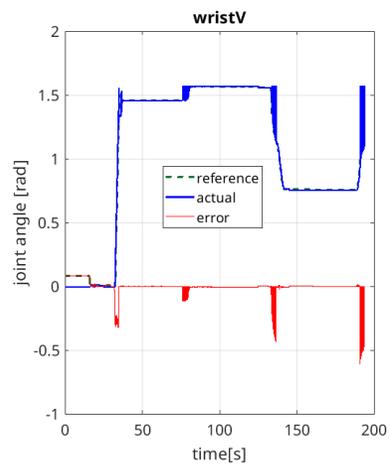
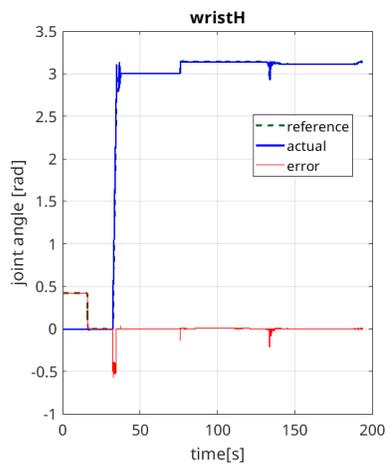
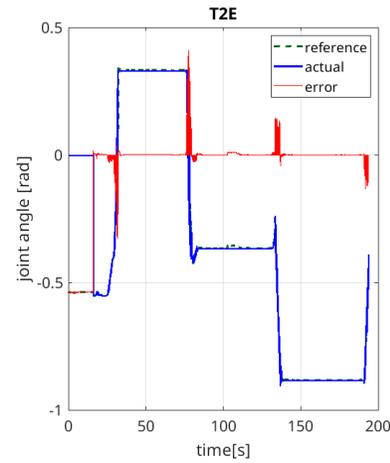
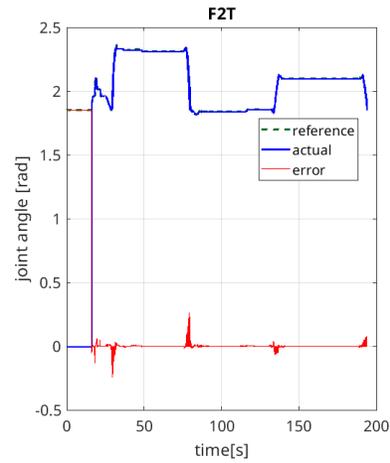
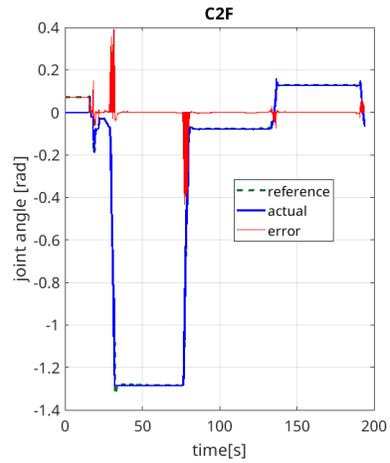
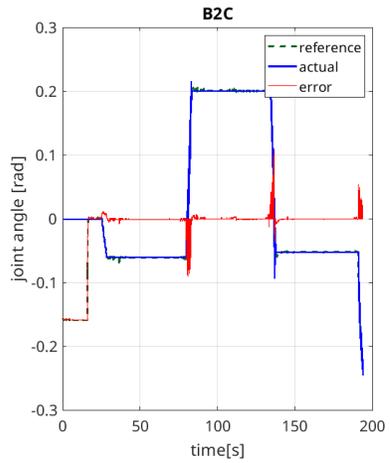


Counterweight

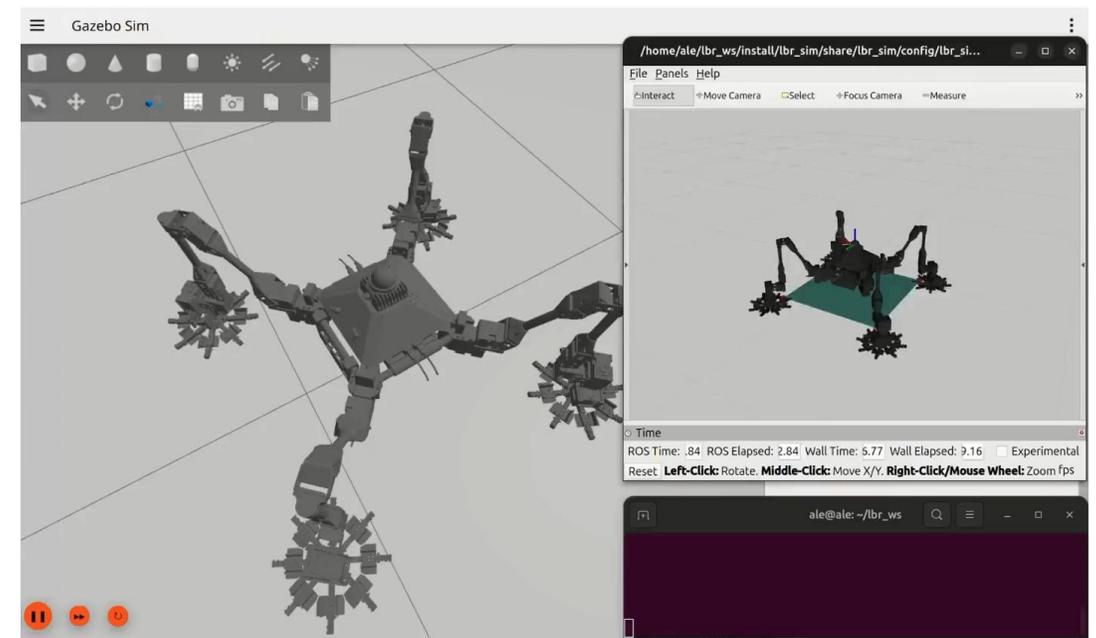
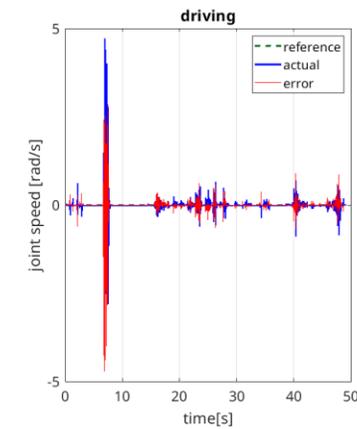
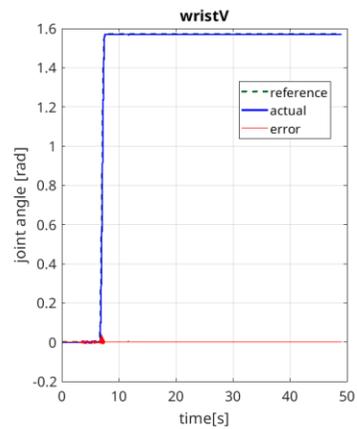
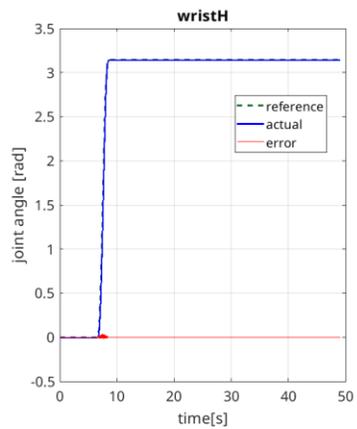
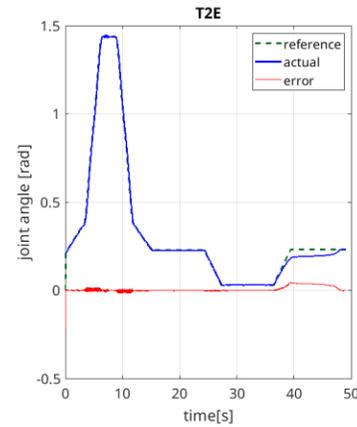
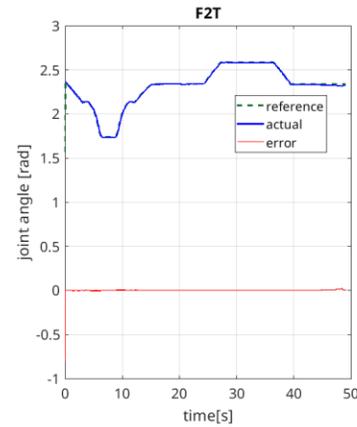
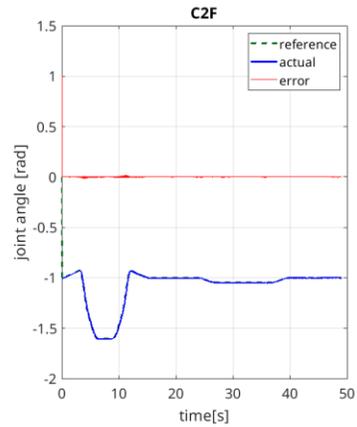
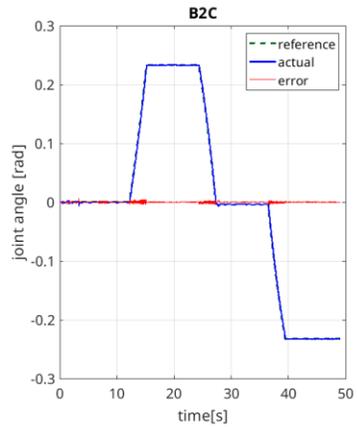




Limb LF: Joint state tracking performance

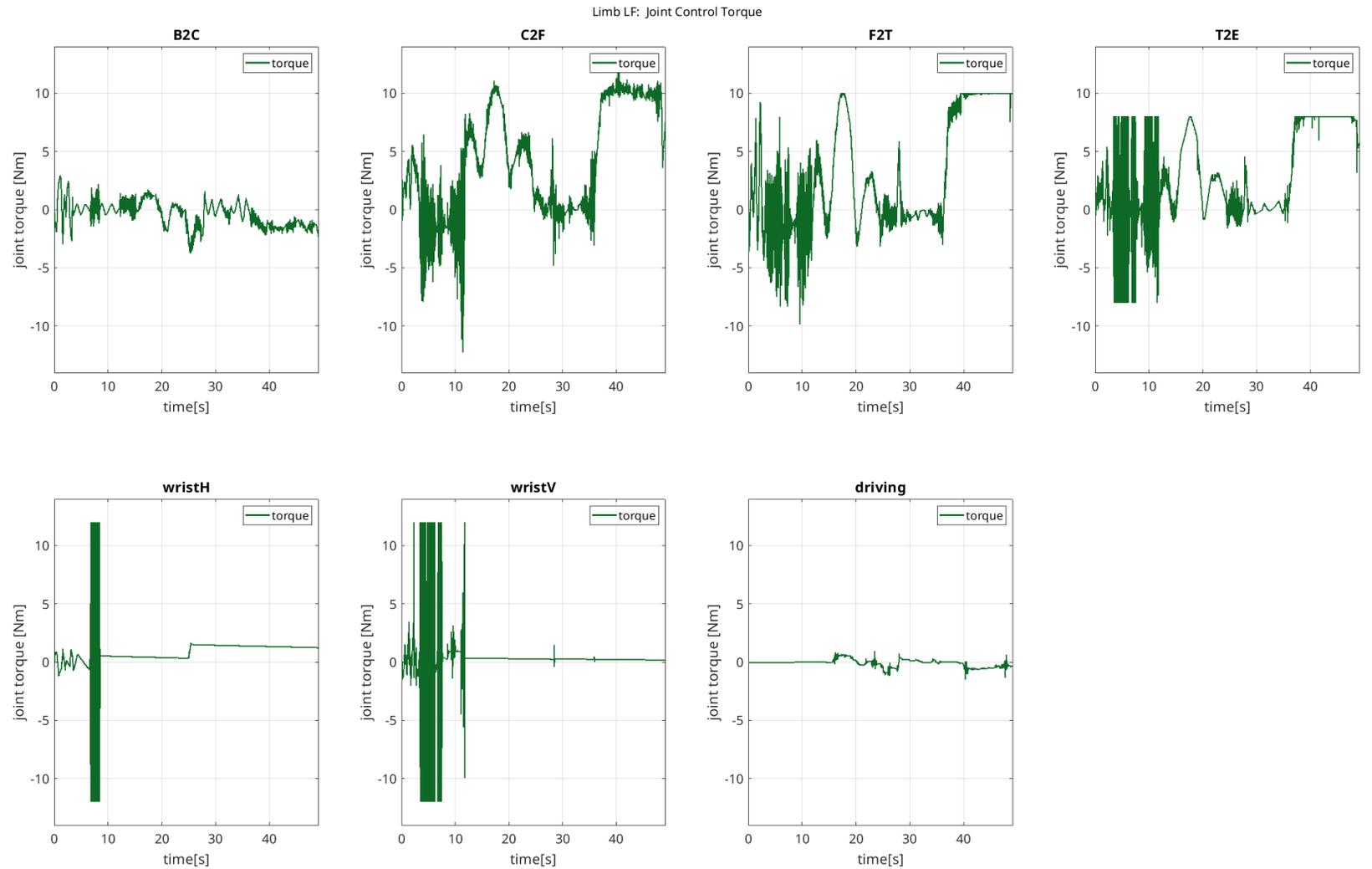
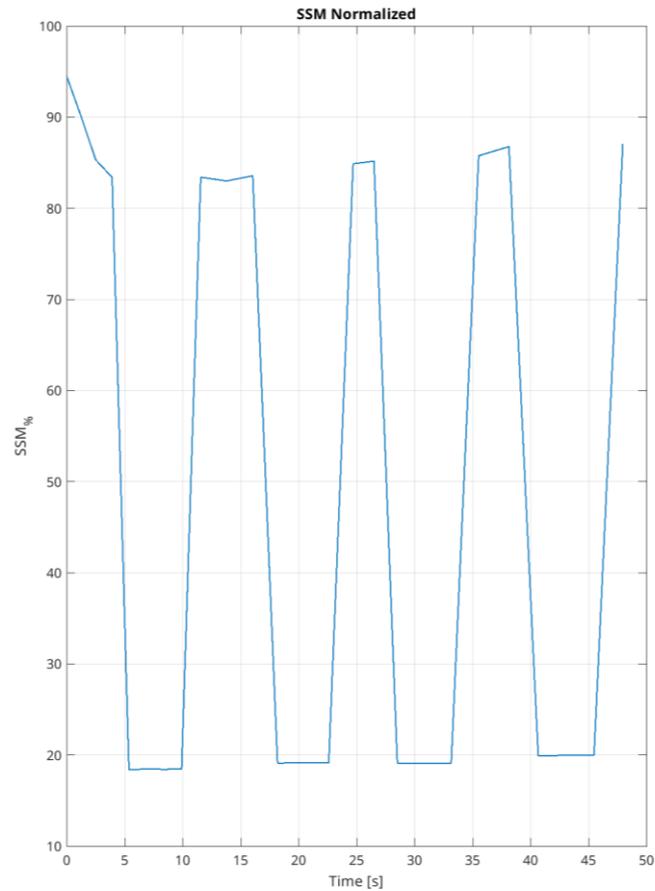


Limb LF: Joint state tracking performance

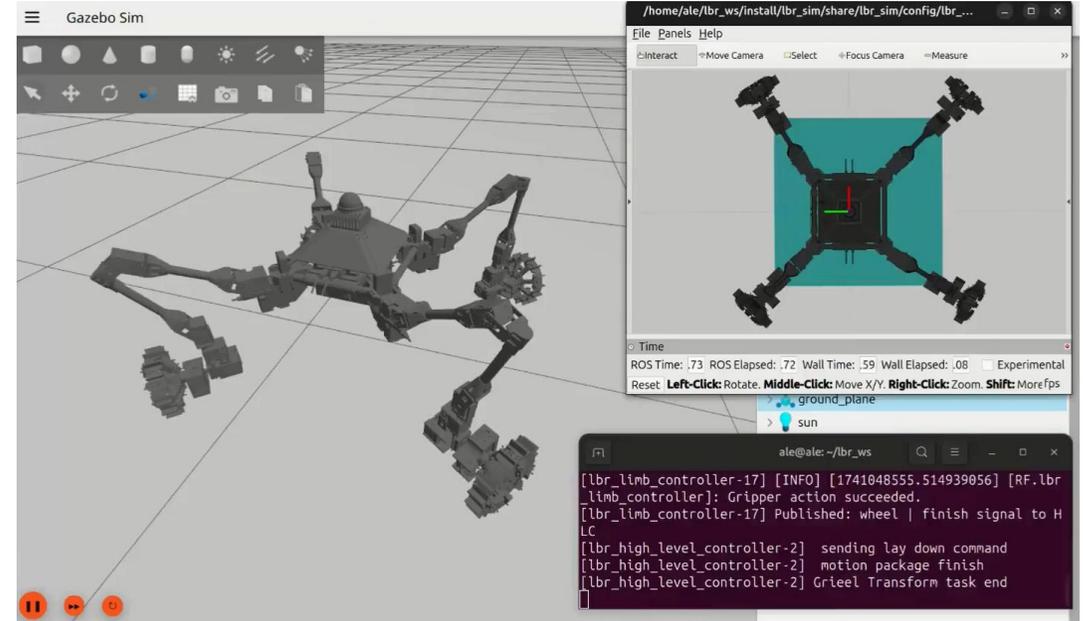
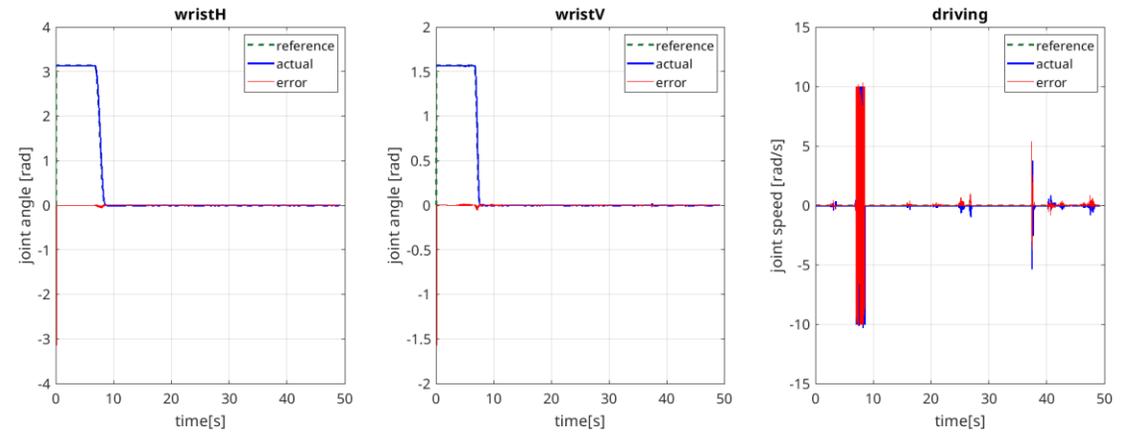
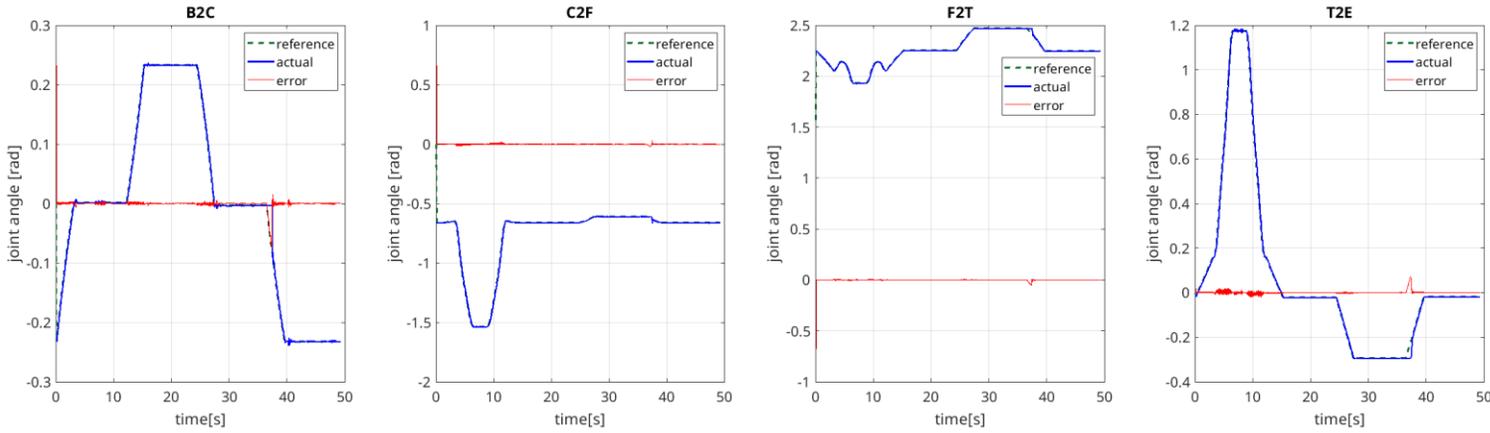


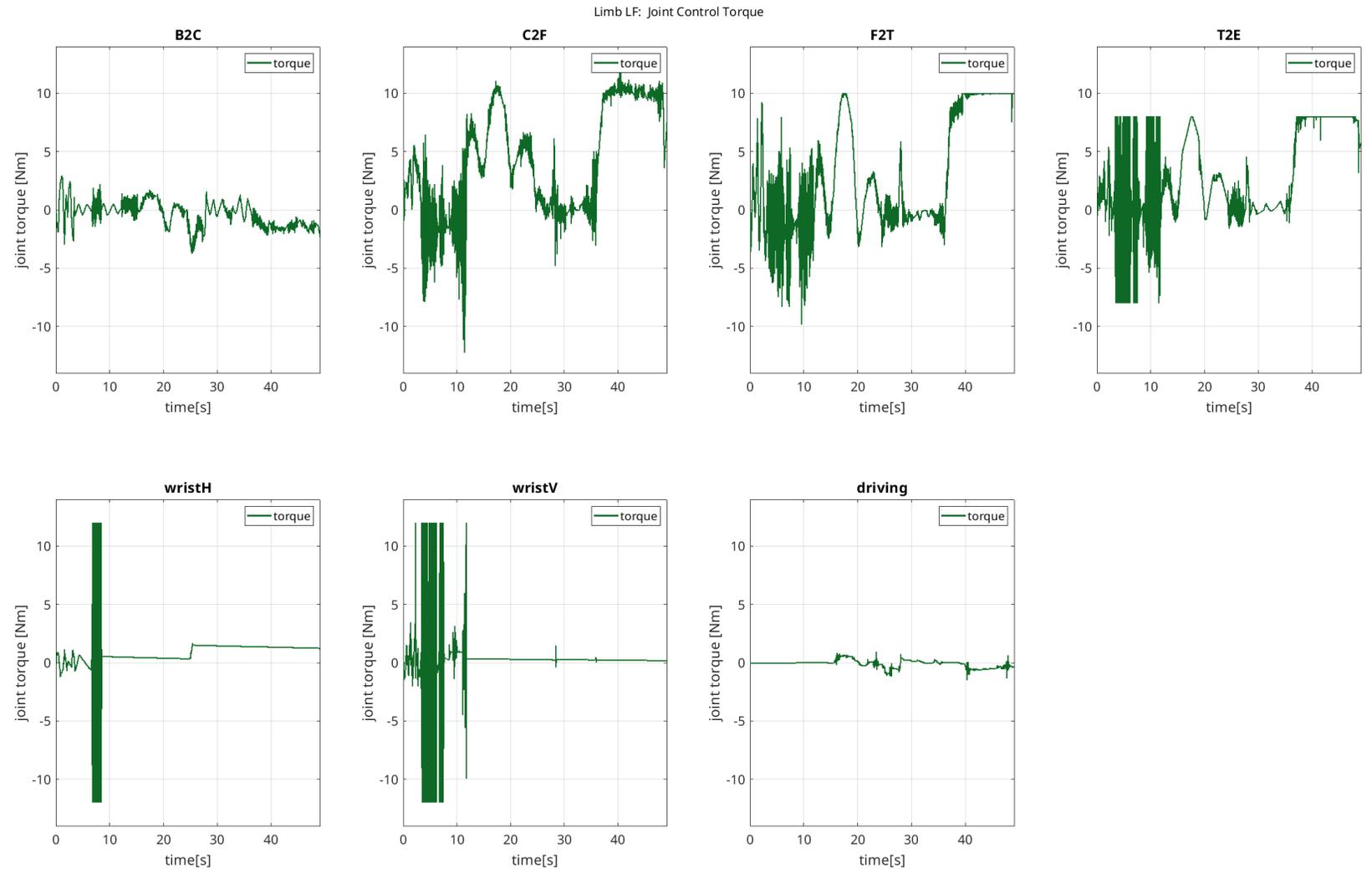
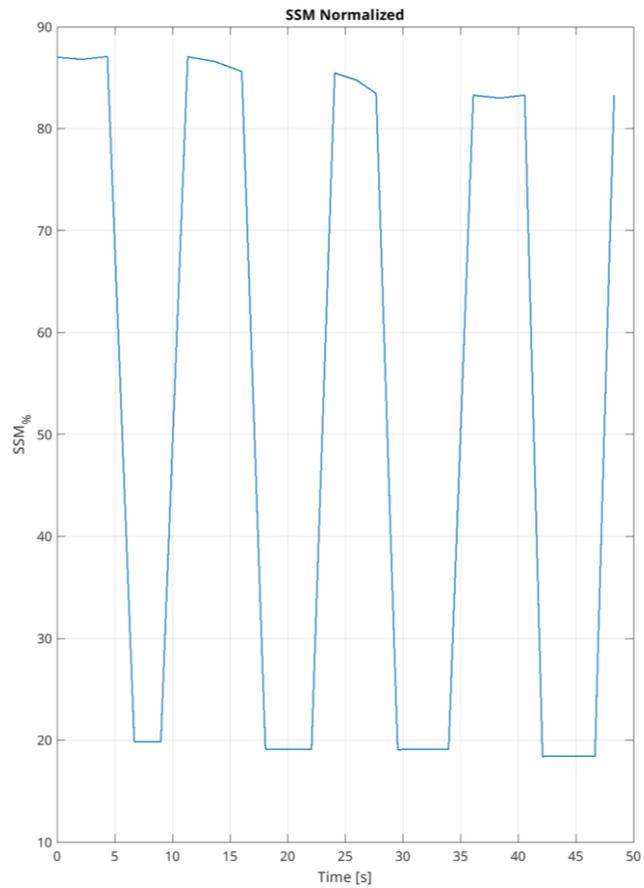
# Results

## Simulations: G2W



Limb LF: Joint state tracking performance

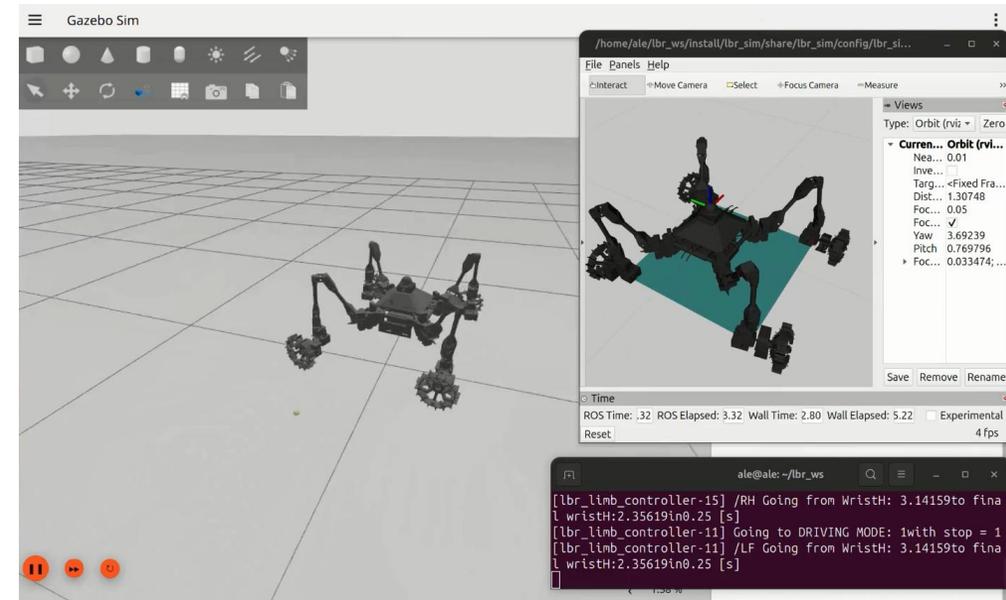
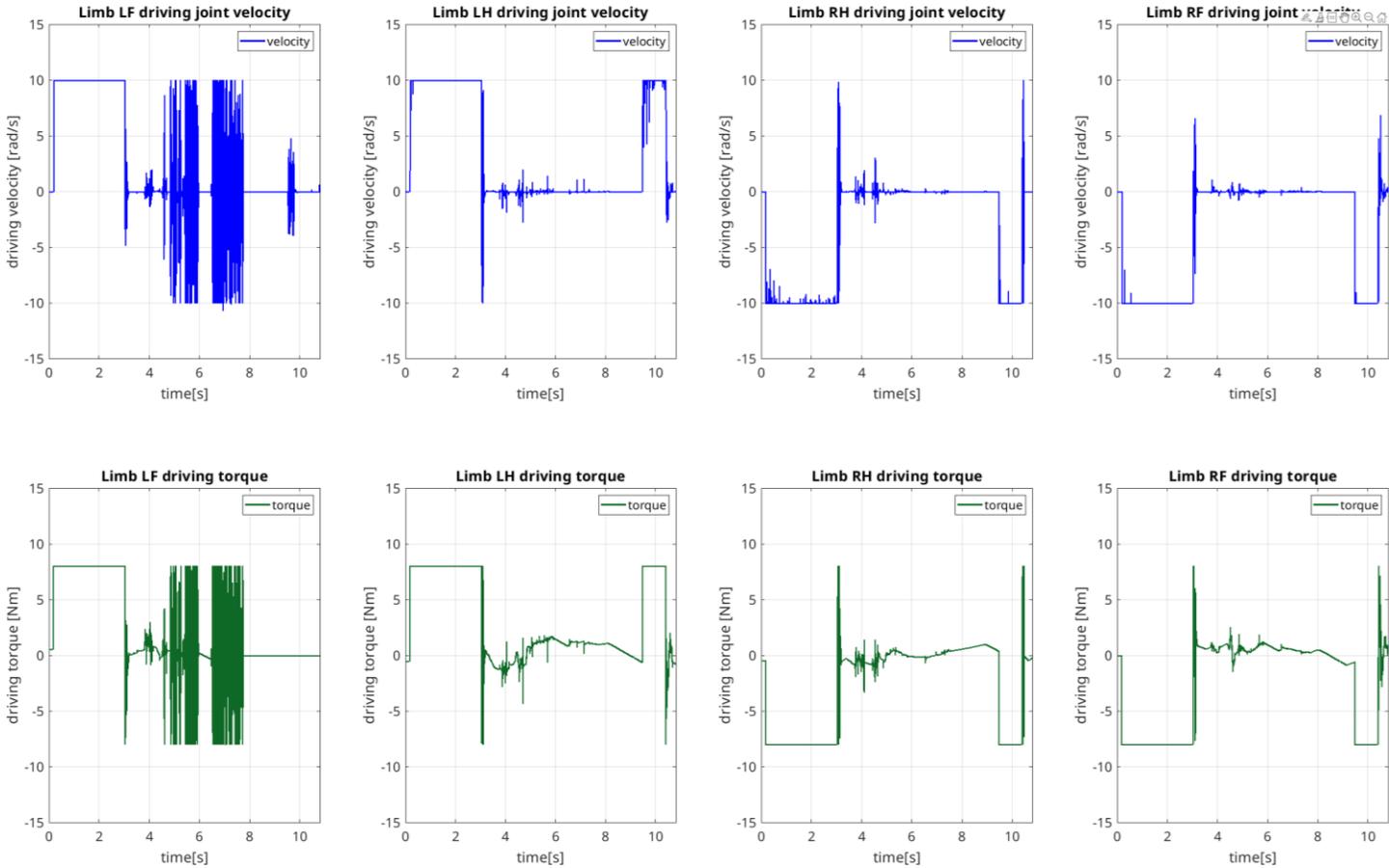




# Results

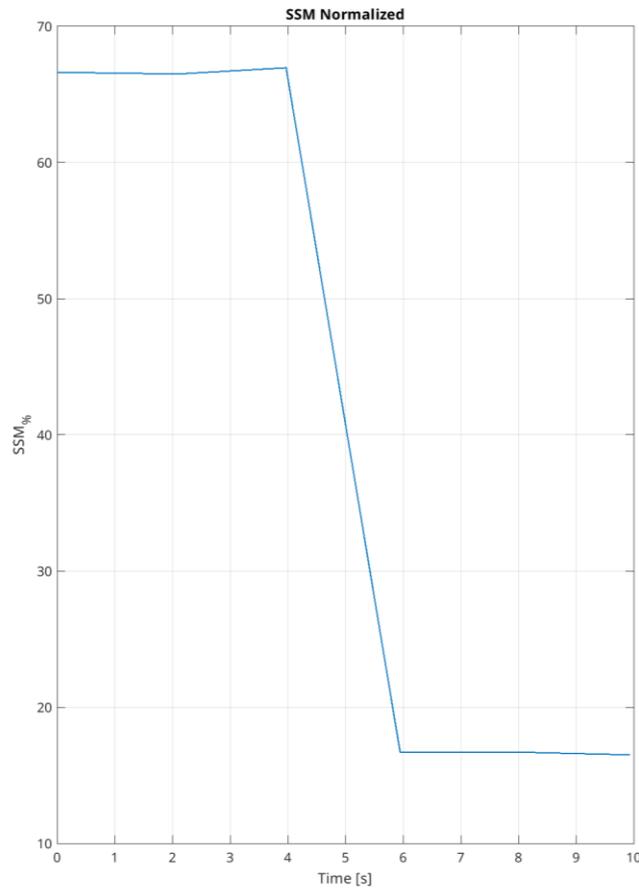
## Simulations: Driving

Driving Velocity tracking performance

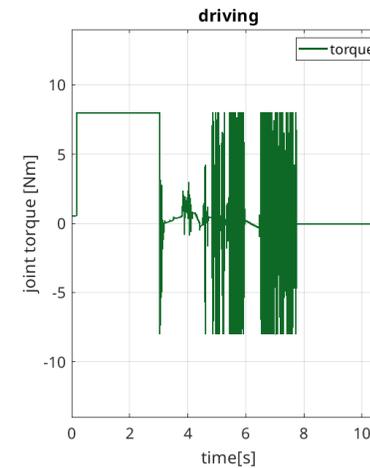
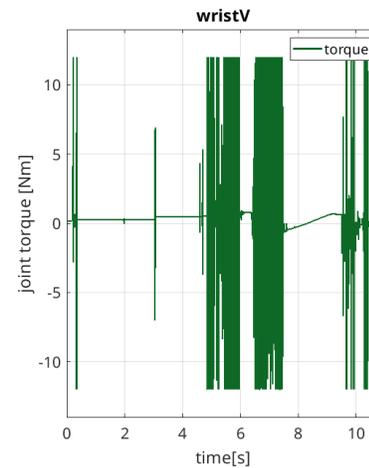
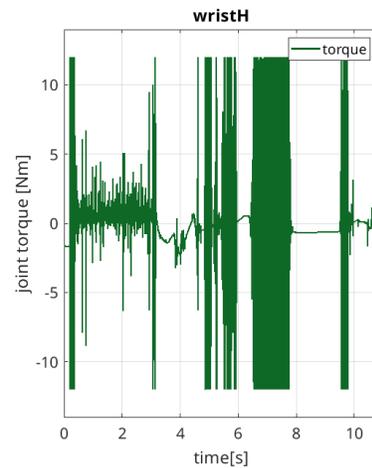
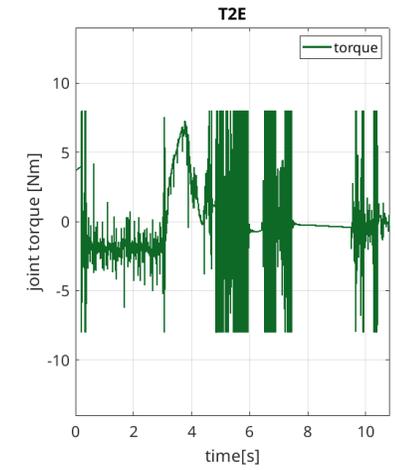
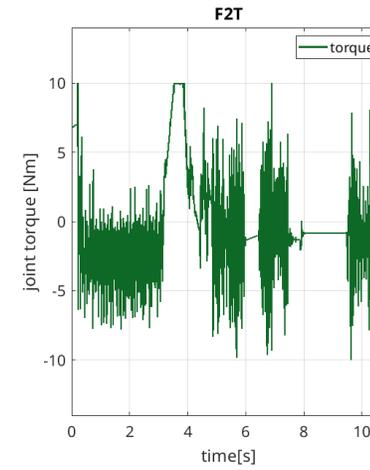
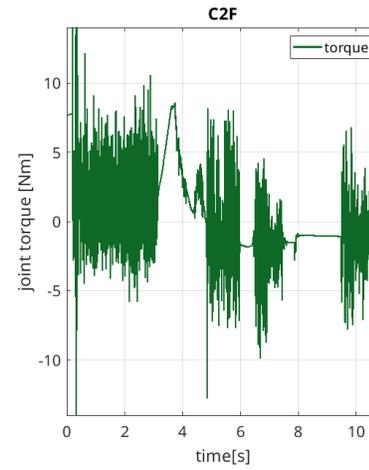
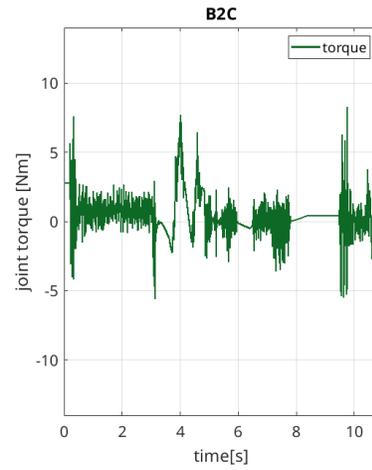


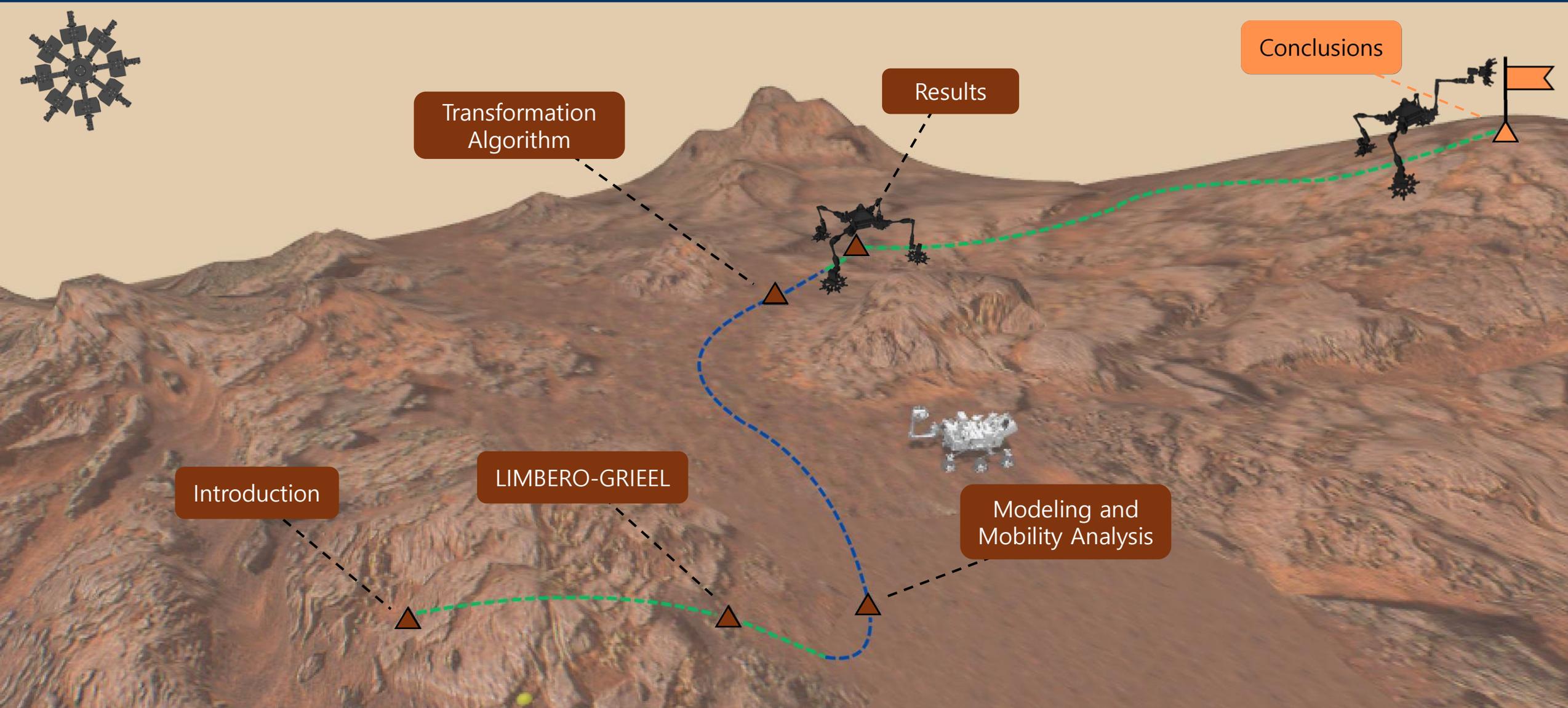
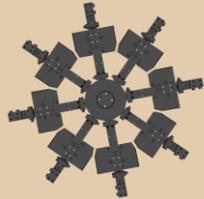
# Results

## Simulations: Driving



Limb LF: Joint Control Torque



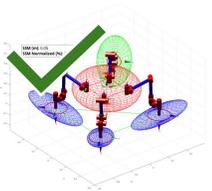




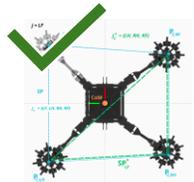
Multilayered motion controller architecture



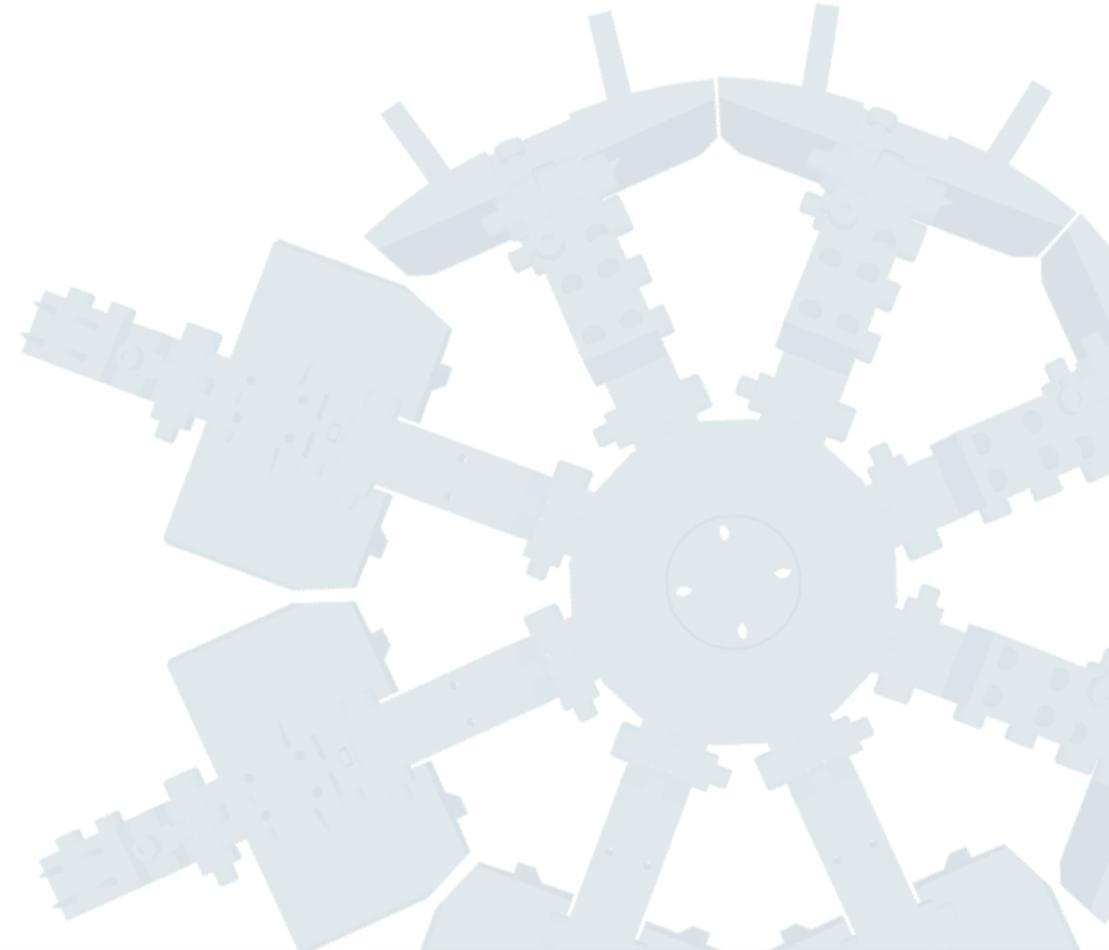
Simulation environment



Dexterity analysis (BME)



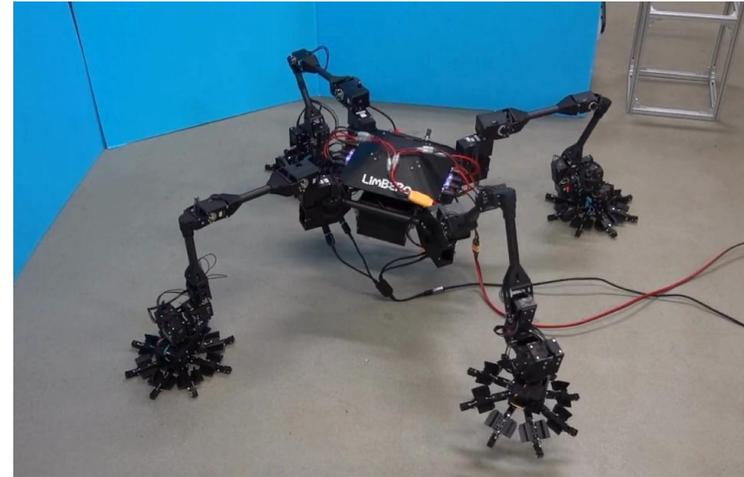
Reliable transformation algorithm



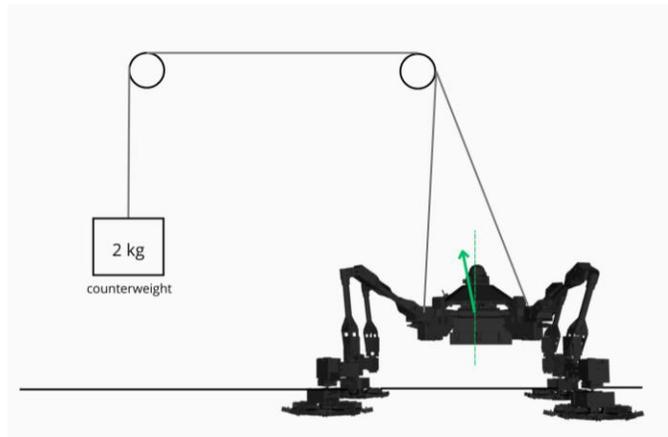
## Contact estimation



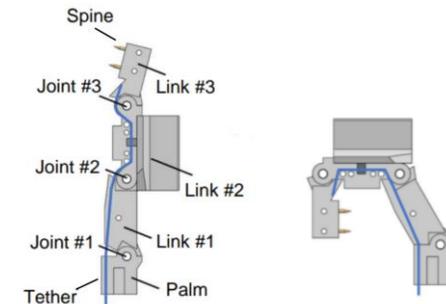
## Joints motor dimensioning



## Counterweight

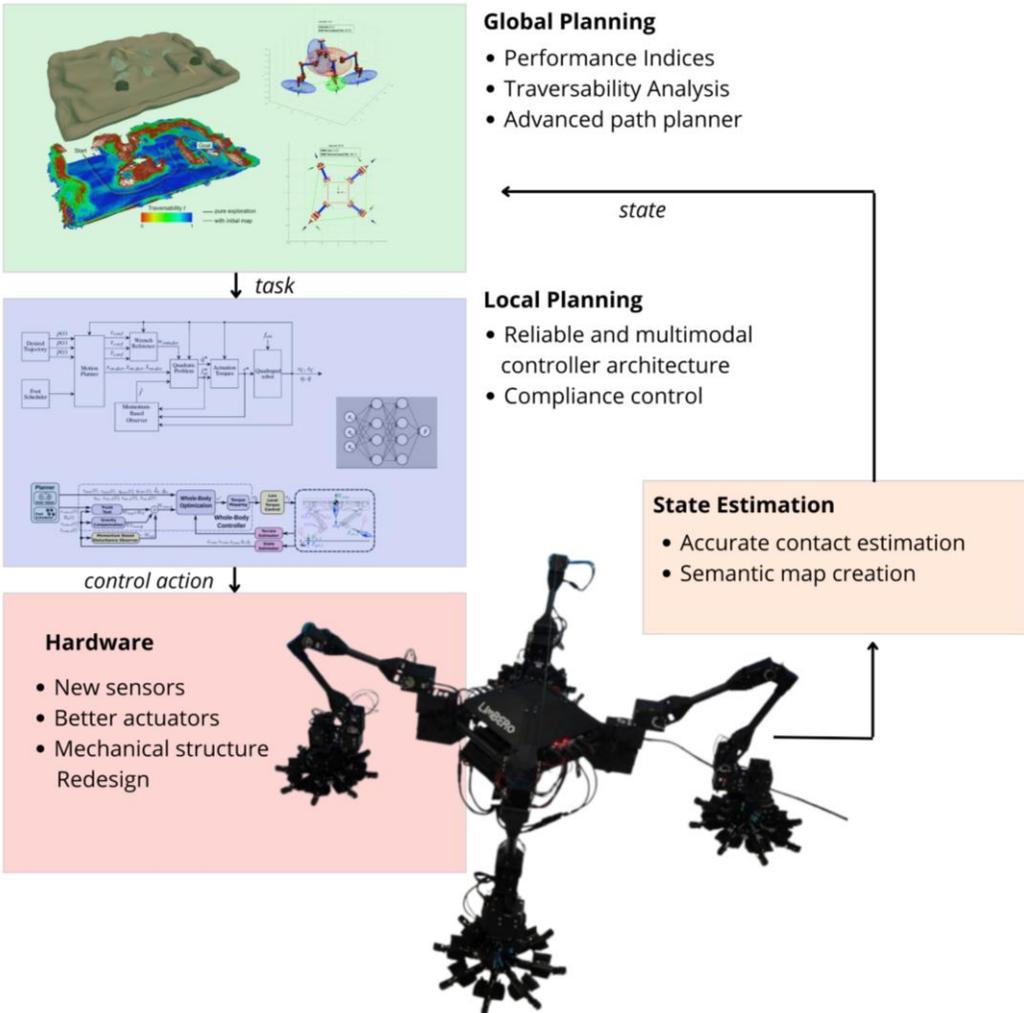


## Unknown GRIEEL module state



Gripper or Wheel Mode?

## Roadmap



## Local Planning (Controller)

- Low-level controllers such as Whole Body, Impedance or Data Driven

## Global Planning

- High-level traversability analysis
- optimal path (foothold) generation
- Autonomous mission planning
- Performance indices

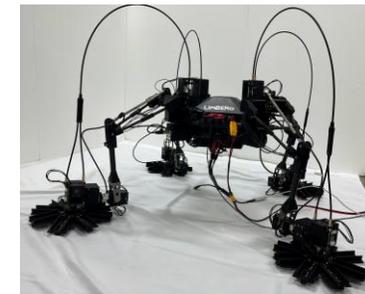
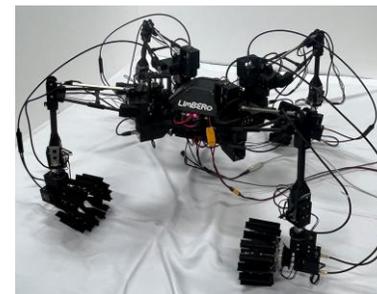
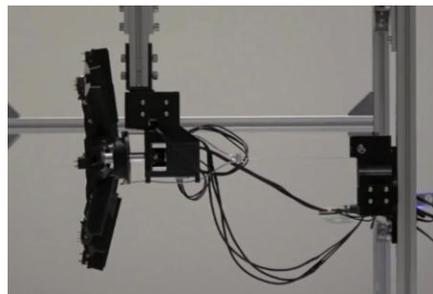
## Hardware

- New sensors
- Proper actuators
- Mechanical structure

## Software

- Independent GRIEEL architecture
- New simulator

## LIMBERO-GRIEEL v2



***THANKS FOR LISTENING***

QUESTIONS or CURIOSITIES ?



**POLITECNICO**  
MILANO 1863



**TOHOKU**  
UNIVERSITY

